

# *Nucleon Form Factors*

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# *Nucleon Form Factors*

## *Introduction*

- Definition
- Formalism
- Interpretation & Utility

## *Data*

- ▷ Early Results
- ▷ Current Status

## *Measurements*

- ▷ Techniques
- ▷ Limitations

## *Theory Models*

## *Measurements at JLab*

# Introduction: Why Form Factors?

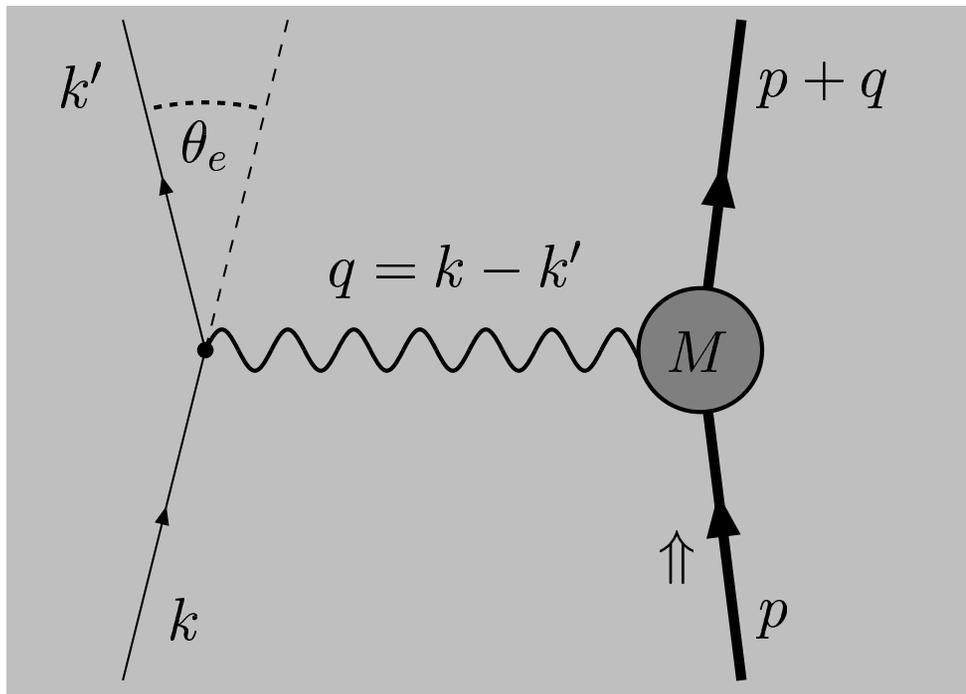
**Mott Cross Section** for spin-dependent elastic scattering of **point-like** particles, recoil free approximation:

$$\left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}} = \frac{4Z^2\alpha^2(\hbar c)^2 E'^2}{|\vec{q}c|^4} \cos^2 \frac{\theta}{2}$$

**But: Proton, Neutron are *not* point-like!**

- ⇒ Introduce phenomenological functions to describe difference between **understood** model and **observed** reality
- ⇒ Test new descriptions by matching to observed **form factors** or **structure functions**

# Interjection: Scattering Kinematics



$$k = (E, \vec{k}), k' = (E', \vec{k}'), \text{ etc.}$$

Momentum Transfer  
("Virtuality")

$$Q^2 = -q^2$$

for elastically scattering  $m$   
off mass  $M$  with  $m \ll M$ :

$$Q^2 = 2M(E - E')$$

# *Interjection: Scattering Kinematics*

## Requirement for Elastic Scattering:

relativistic mass before = relativistic mass after

$$(\underline{\mathbf{M}})^2 = (\underline{\mathbf{M}} + \underline{\mathbf{q}})^2$$

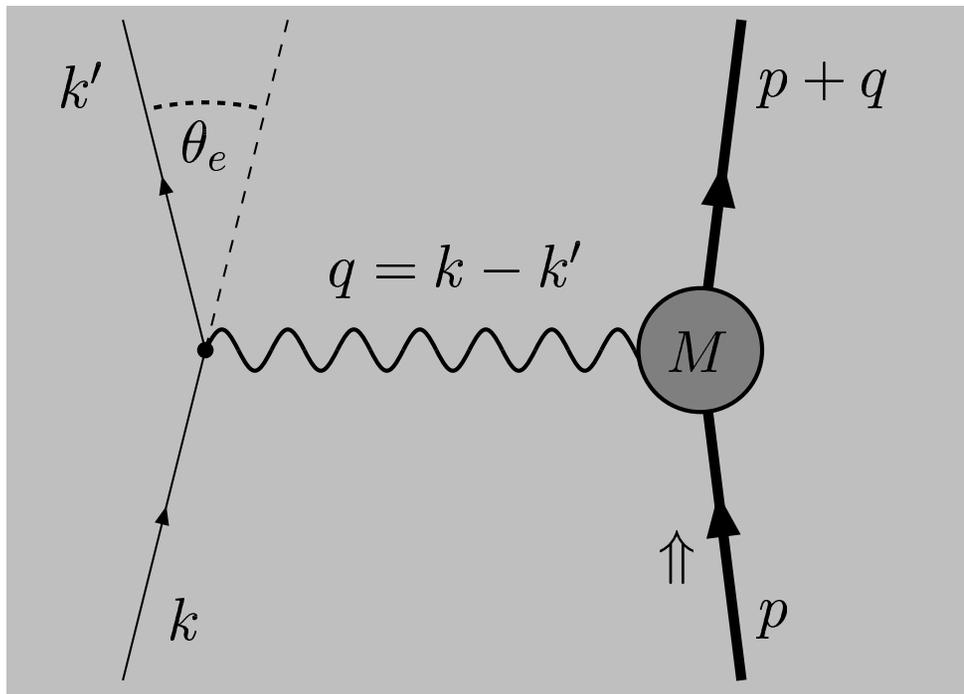
$$M^2 = (\underline{\mathbf{M}} - \underline{\mathbf{Q}})^2$$

$$= M^2 + Q^2 - 2 \underline{\mathbf{M}} \cdot \underline{\mathbf{Q}}$$

$$Q^2 = 2 (M, 0) \cdot (E - E', \vec{k} - \vec{k}')$$

$$= 2 M (E - E')$$

# Interjection: Scattering Kinematics



Momentum Transfer  
("Virtuality")

$$Q^2 = -q^2$$

for elastically scattering  $m$   
off mass  $M$  with  $m \ll M$ :

$$Q^2 = 2M(E - E')$$

$k = (E, \vec{k})$ ,  $k' = (E', \vec{k}')$ , etc.

## Generalization:

interpret *inelastic* scattering off nucleon as *elastic*  
scattering off constituent with momentum fraction  $x$

$$Q^2 = 2xM(E - E') \quad \text{or} \quad x = \frac{Q^2}{2M(E - E')}$$

# Introduction: Formalism

## Sachs Form Factors for Elastic Scattering

$$\frac{d\sigma}{d\Omega} = \left( \frac{d\sigma}{d\Omega} \right)_{\text{Mott}} \times \left[ \frac{G_E^2 + \tau G_M^2}{1 + \tau} + 2\tau G_M^2 \tan^2 \frac{\theta_e}{2} \right]$$

$G_E, G_M$  depend on  $Q^2$  !

$$\tau = \frac{Q^2}{4M^2}$$

### Limiting Case

point-like *probe* ( $Q^2 = 0$ )

Proton:  $G_E^p = 1$        $G_M^p = 2.79 \mu_N$

Neutron:  $G_E^n = 0$        $G_M^n = -1.91 \mu_N$

charge

magnetic moment

# *Introduction: Interpretation*

In Breit frame (non-relativistic limit):

Fourier Transform of **Charge, Current Distribution**

$$F(\vec{q}) = \int e^{i\vec{q}\vec{x}/\hbar} f(\vec{x}) d^3x$$

Momentum Space

Coordinate Space

# *Aside: Structure Functions*

Form Factors for *Elastic* Scattering Only

More General:

Structure Functions  $F_1(x, Q^2)$  and  $F_2(x, Q^2)$

In the Limit of Elastic Scattering ( $x \rightarrow 1$ ):

$$G_E(Q^2) = F_1(Q^2) - \tau\mu F_2(Q^2)$$

$$G_M(Q^2) = F_1(Q^2) + \mu F_2(Q^2)$$

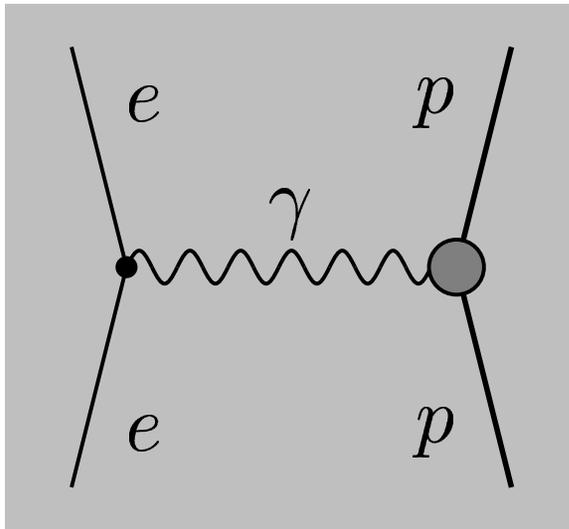
Also:

*Spin* Structure Functions  $g_1(x, Q^2)$  and  $g_2(x, Q^2)$

# Aside: Weak Form Factors

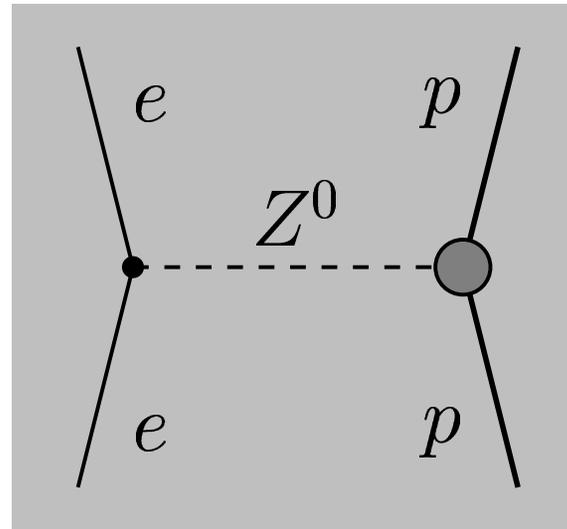
Inclusion of Weak Interaction in  $e - p$  Scattering:

EM Interaction



$G_E^\gamma, G_M^\gamma$

Weak Interaction



$G_E^{Z^0}, G_M^{Z^0}, G_A^{Z^0}$

Cross Section  $\sigma = |M_\gamma + M_{Z^0}|^2 \quad \frac{M_\gamma \times M_Z}{M_\gamma^2} \sim 1/20\,000$

Interference Term  $M_\gamma \times M_{Z^0}$  Violates Parity

# *Nucleon Form Factors: Introduction*

Form Factors:

spacial extent of charge & current (sub-structure)

→ anomalous magnetic moment

- Fundamental Quantities
- Test of QCD
- Required for Study of Other Physics
  - *Few-Body Structure Functions*
  -

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## *Data*

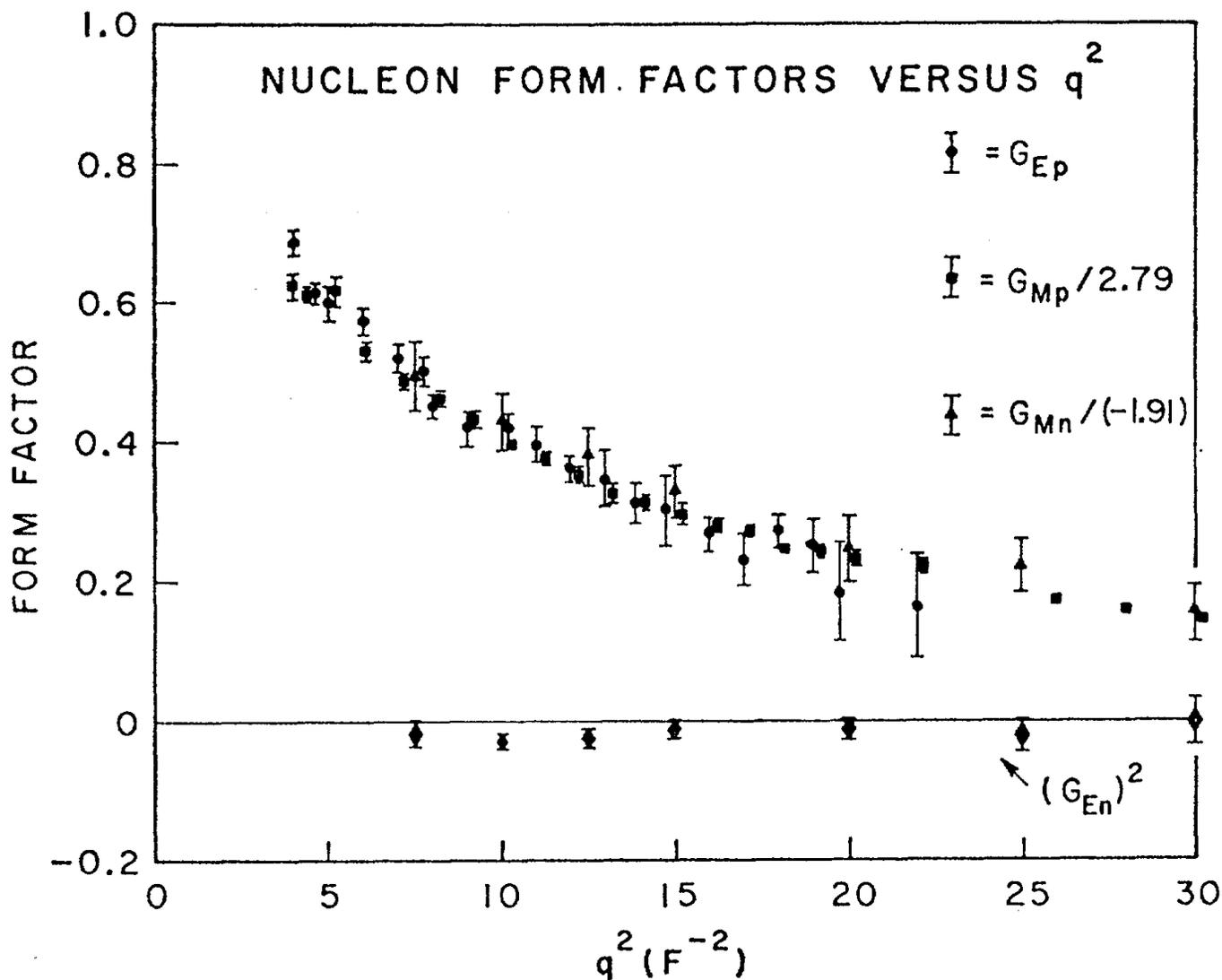
- Early Results
- Current Status

## *Measurements*

- ▷ Techniques
- ▷ Limitations

## *Measurements at JLab*

# Data Surprise: Similar $Q^2$ Behavior



Phys. Rev. 139,  
B458 (1965)

$30\text{fm}^{-2} \simeq 1.17\text{GeV}^2$

$$G_E^p \approx G_M^p/\mu_p \approx G_M^n/\mu_n \quad G_E^n \approx 0$$

# Basic Approximation: Dipole Fit

$$G(Q^2) \approx G(Q^2=0) \times G_D(Q^2)$$

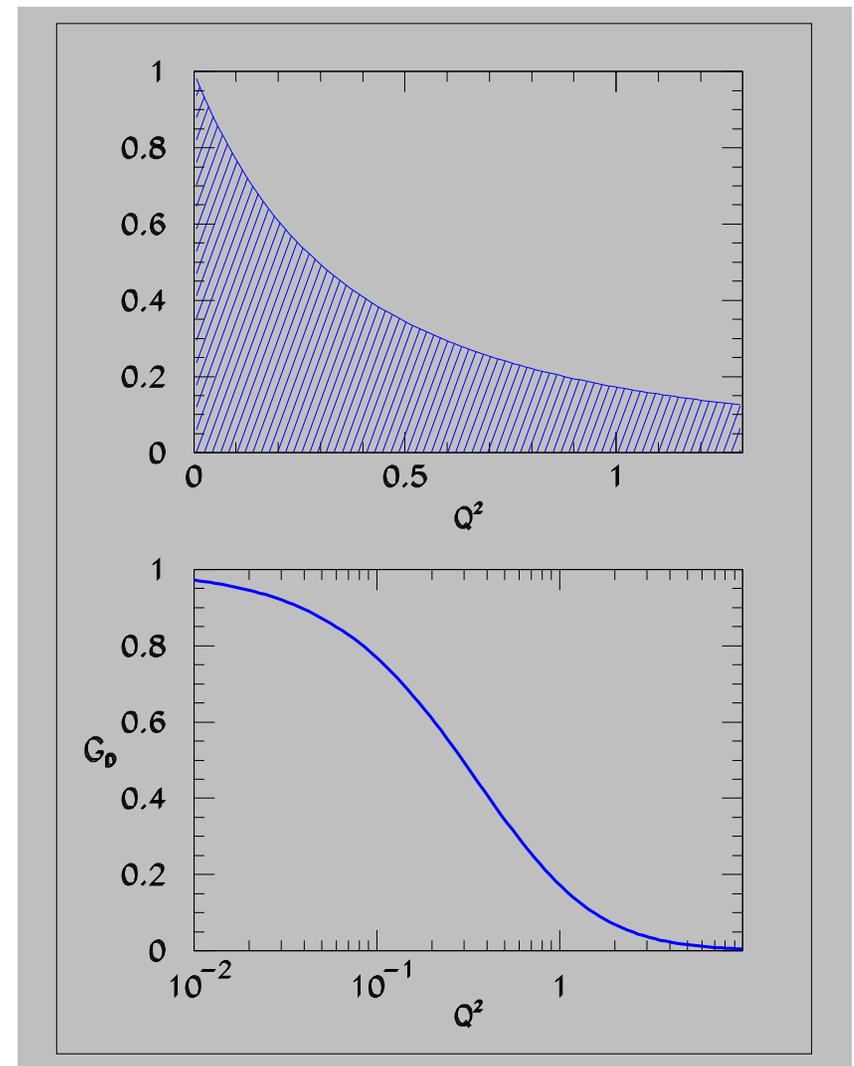
Fitted to Data:

$$G_D = \left(1 + \frac{Q^2}{0.71}\right)^{-2}$$

Based on FT of Exponential Charge Distribution

$$\sim e^{-\alpha r}$$

With  $\alpha = 4.27 \text{ fm}^{-1}$



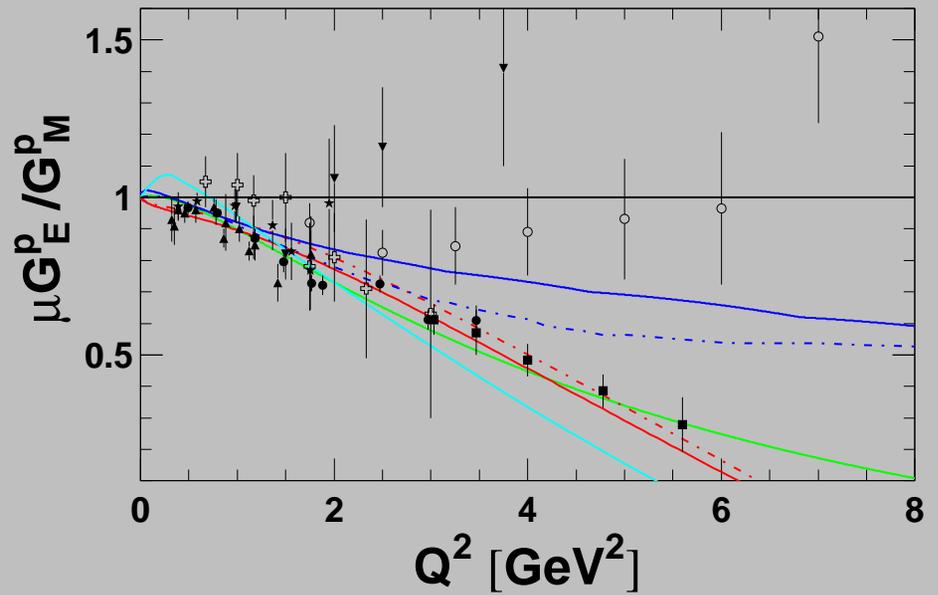
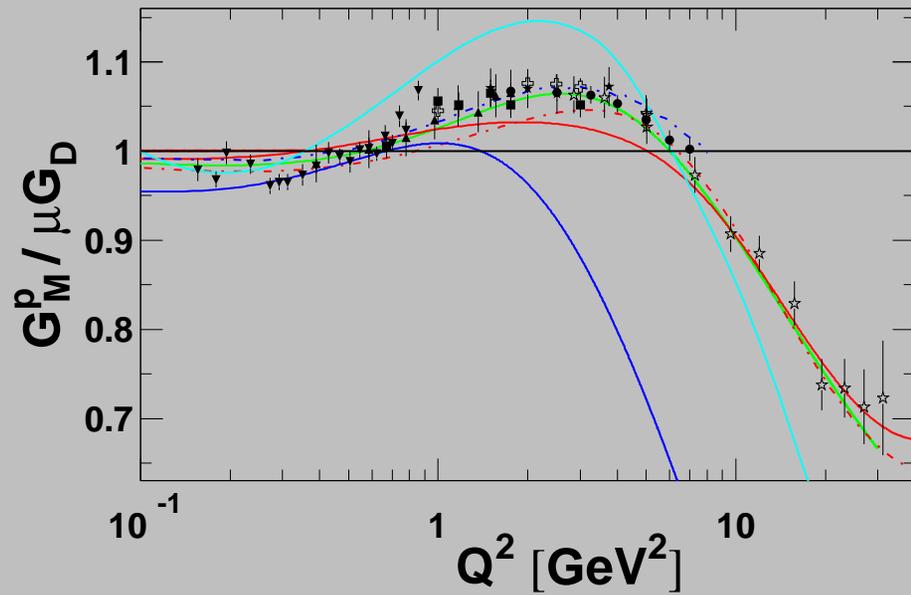
# Current Status

## Data:

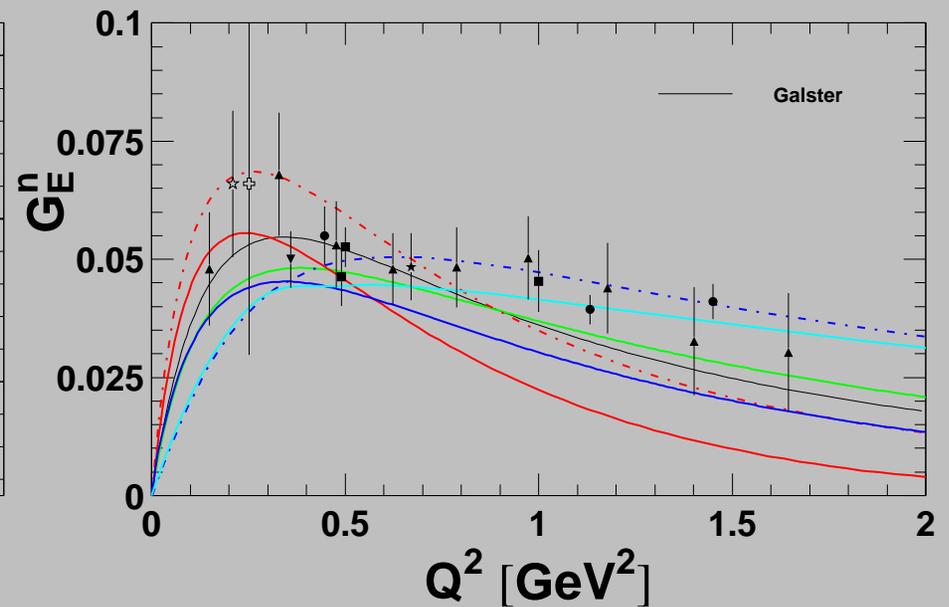
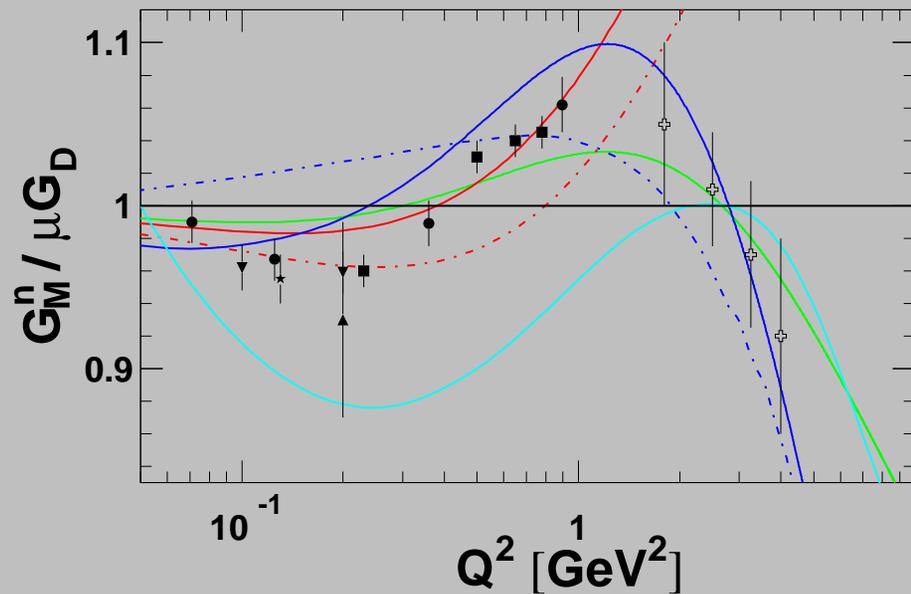
- All Form Factors Measured ( $G_E^p$ ,  $G_M^p$ ,  $G_E^n$ ,  $G_M^n$ )
- $0 \leq Q^2 < \sim 10 \text{ GeV}^2$

## Models:

- Several QCD-based Models
  - *Vector Meson Dominance pQCD*
  - *light front CQM, Goldstone Boson Exchange CQM*
  - *Solitons*
- **None** Well Describe all Form Factors over *Entire* Measured Range



- VMD + pQCD (Lomon 2002)
- PFSA CQM GBE
- - - Soliton (Holzwarth b1)
- - - LF CQM qFF (Cardarelli)
- Soliton (Holzwarth b2)
- LF CQM  $\pi$  (Miller)



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# Form Factor Measurements

## Traditional Methods:

- Cross Section Based

- Rosenbluth Separation

$$\frac{d\sigma}{d\Omega} \sim \frac{G_E^2 + \tau G_M^2}{1 + \tau} + 2\tau G_M^2 \tan^2 \frac{\theta_e}{2}$$

- Highly Sensitive to Wavefunction Models, RCs

## Polarization-Based Methods:

- Polarization Observables (asymmetry, LT-ratio)

- Complex Setups

- Asymmetry Measurements Require Absolute Polarization

# Rosenbluth Separation – Formalism

Recall:

$$\frac{d\sigma}{d\Omega} = \left( \frac{d\sigma}{d\Omega} \right)_{\text{Mott}} \times \left[ \frac{G_E^2 + \tau G_M^2}{1 + \tau} + 2\tau G_M^2 \tan^2 \frac{\theta_e}{2} \right]$$

Alternatively:

$$\frac{d\sigma}{d\Omega} = \frac{\sigma_{\text{Mott}}}{\epsilon (1 + \tau)} \times \underbrace{\left[ \tau G_M^2(Q^2) + \epsilon G_E^2(Q^2) \right]}$$

**Problem:**  
as  $Q^2$  increases,  
 $\tau G_M^2$  dominates

depends linearly in  $\epsilon$  on  $G_E$ ,  
but fixed contribution from  $G_M$   
 $\Rightarrow$  vary  $\epsilon$  but keep  $Q^2$  fixed

$$\epsilon^{-1} = 1 + 2(1 + \tau) \tan^2(\theta_e/2)$$

$$\tau = \frac{Q^2}{4M^2}$$

*longitudinal polarization of virtual photon*

# Asymmetry Measurement – Formalism

$$\left(\frac{d\sigma}{d\Omega}\right)^{pol} = \left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}} \times \left[ \Sigma + h \mathcal{P}_{\text{target}} \Delta \right]$$

$$\Sigma = \left[ \frac{G_E^2 + \tau G_M^2}{1 + \tau} + 2\tau G_M^2 \tan^2 \frac{\theta_e}{2} \right]$$

$$\Delta = -2 \tan \frac{\theta_e}{2} \sqrt{\frac{\tau}{1 + \tau}} \times \left[ \sqrt{\tau (1 + (1 + \tau) \tan^2 \frac{\theta_e}{2})} \cos \theta^* G_M^2 + G_E G_M \sin \theta^* \cos \phi^* \right]$$

Measurement via Vector Asymmetry  $A^V = \frac{\Delta}{\Sigma} = \frac{\sigma_+ - \sigma_-}{\sigma_+ + \sigma_-}$

# Asymmetry Measurement – Formalism

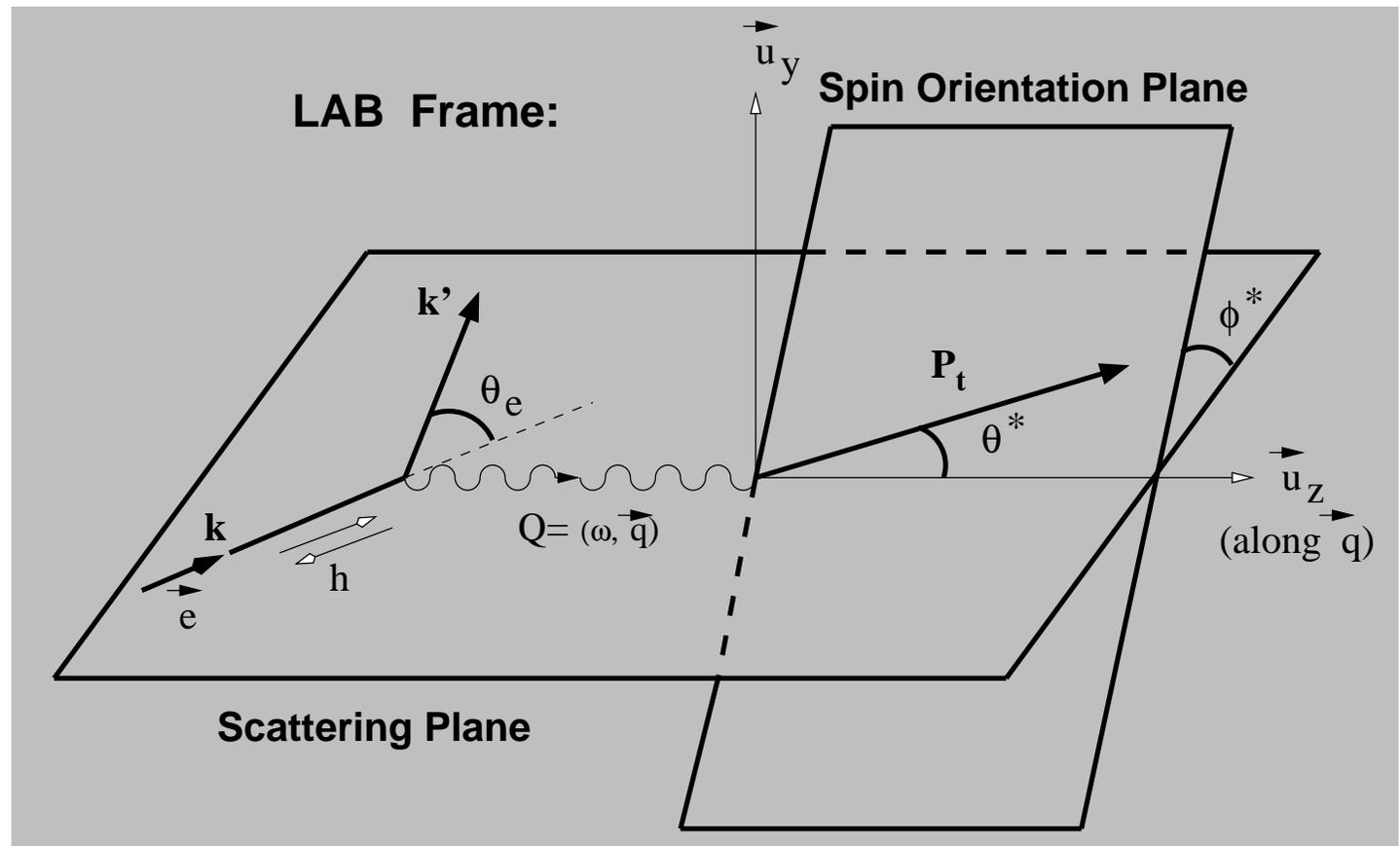
for quasi-free,

$$\mathcal{P}_{\text{target}} \perp \vec{q}$$

$$(\theta^* = 90^\circ)$$

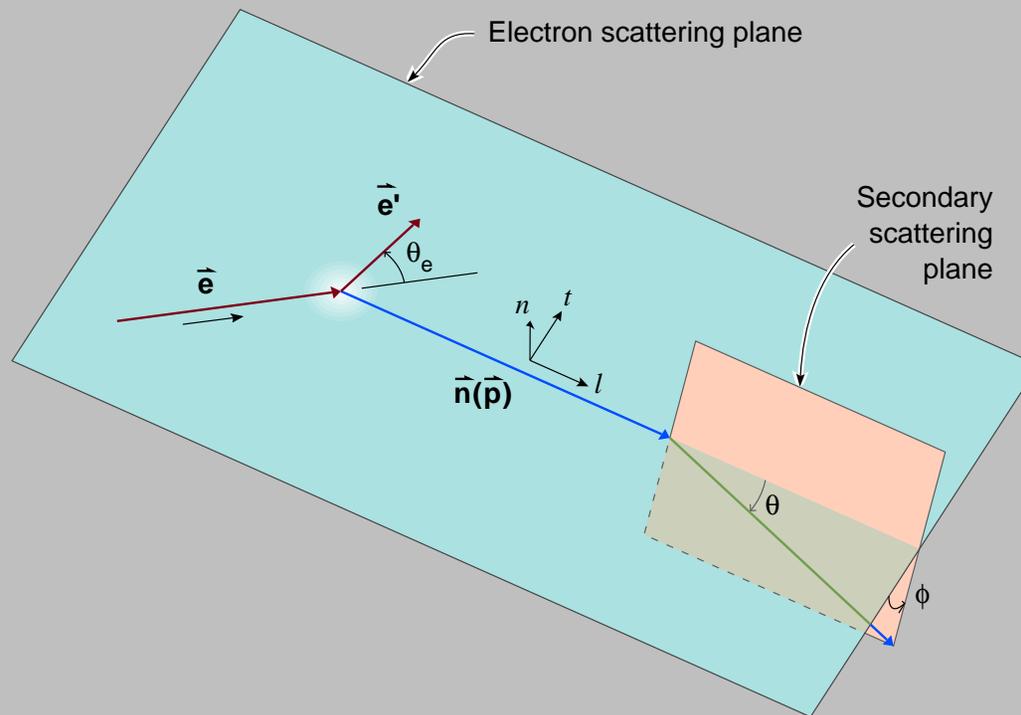
and

$\mathcal{P}_{\text{target}}$  in  
scattering plane  
( $\phi^* = 0$ ),



$$A^V = \frac{-2 \sqrt{\tau(1+\tau)} \tan \frac{\theta_e}{2} G_E G_M}{G_E^2 + \tau [1 + 2(1+\tau) \tan^2 \frac{\theta_e}{2}] G_M^2}$$

# Recoil Polarimetry – Formalism



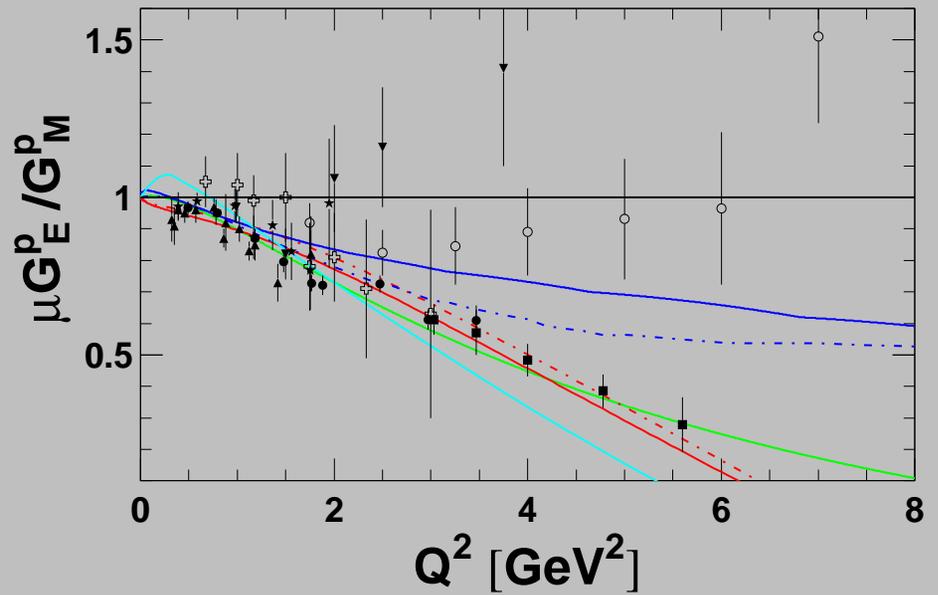
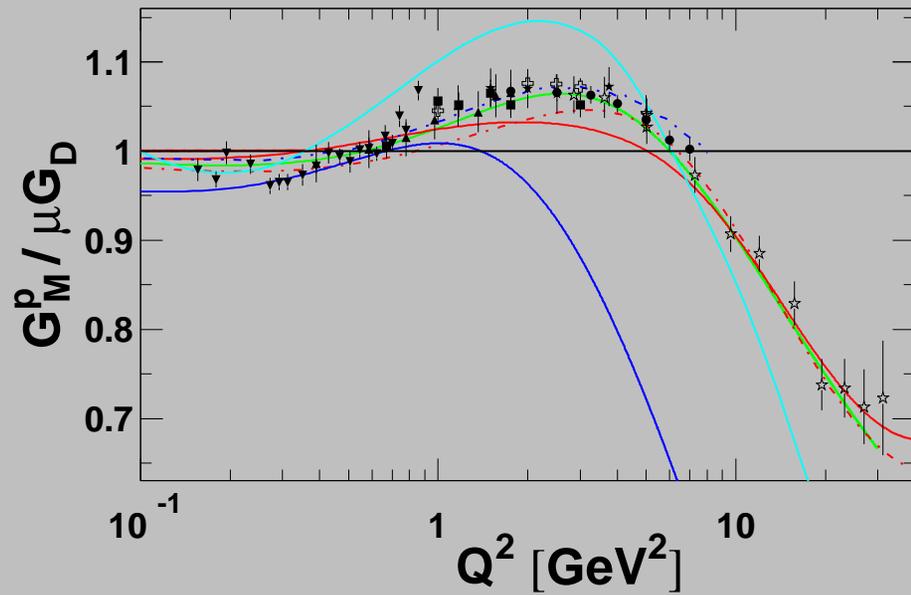
$$I_0 P_n = 0$$

$$I_0 P_t = -2\sqrt{\tau(1+\tau)} G_E G_M \tan(\theta_e/2)$$

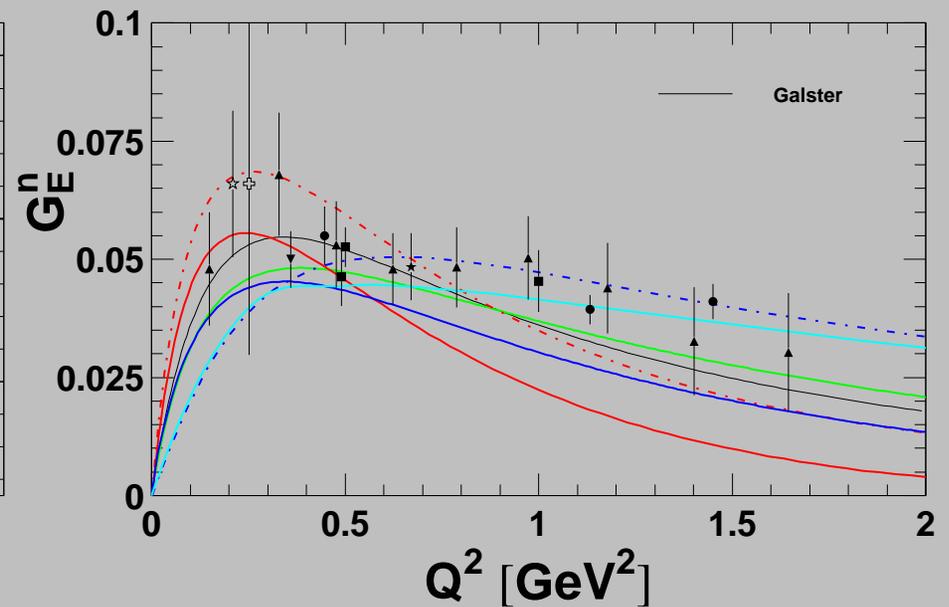
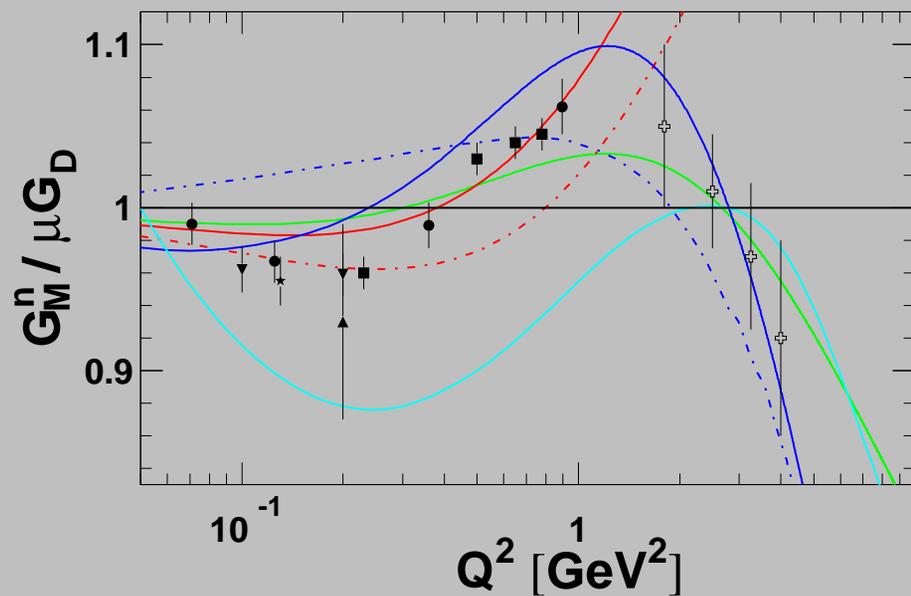
$$I_0 P_l = \frac{1}{M} (E_e + E_{e'}) \sqrt{\tau(1+\tau)} G_M^2 \tan^2(\theta_e/2)$$

$$\frac{G_E}{G_M} = -\frac{P_t (E_e + E_{e'})}{P_l 2M} \tan\left(\frac{\theta_e}{2}\right)$$

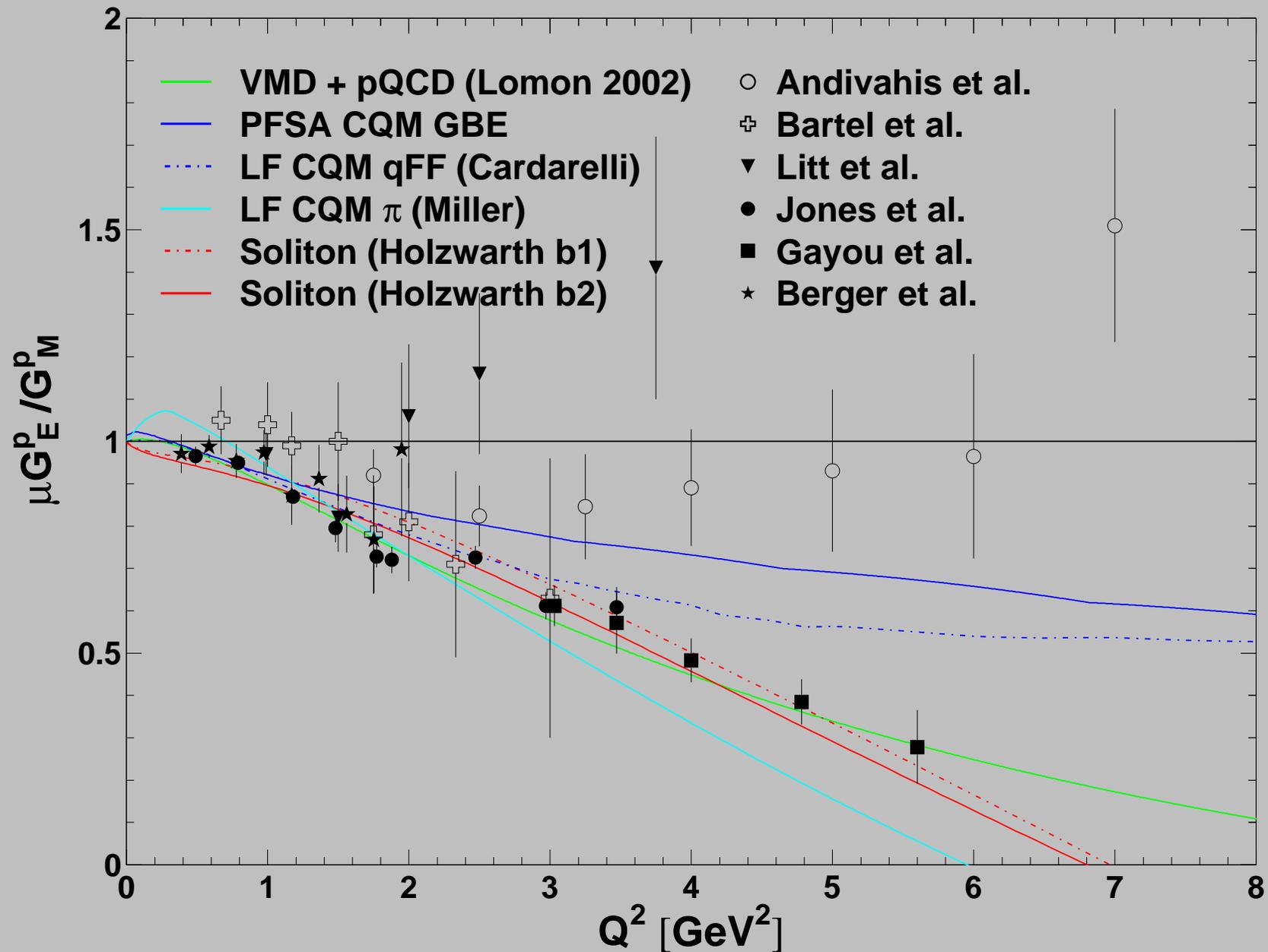
Direct measurement of form factor ratio by measuring the ratio of the transferred polarization  $P_t$  and  $P_l$



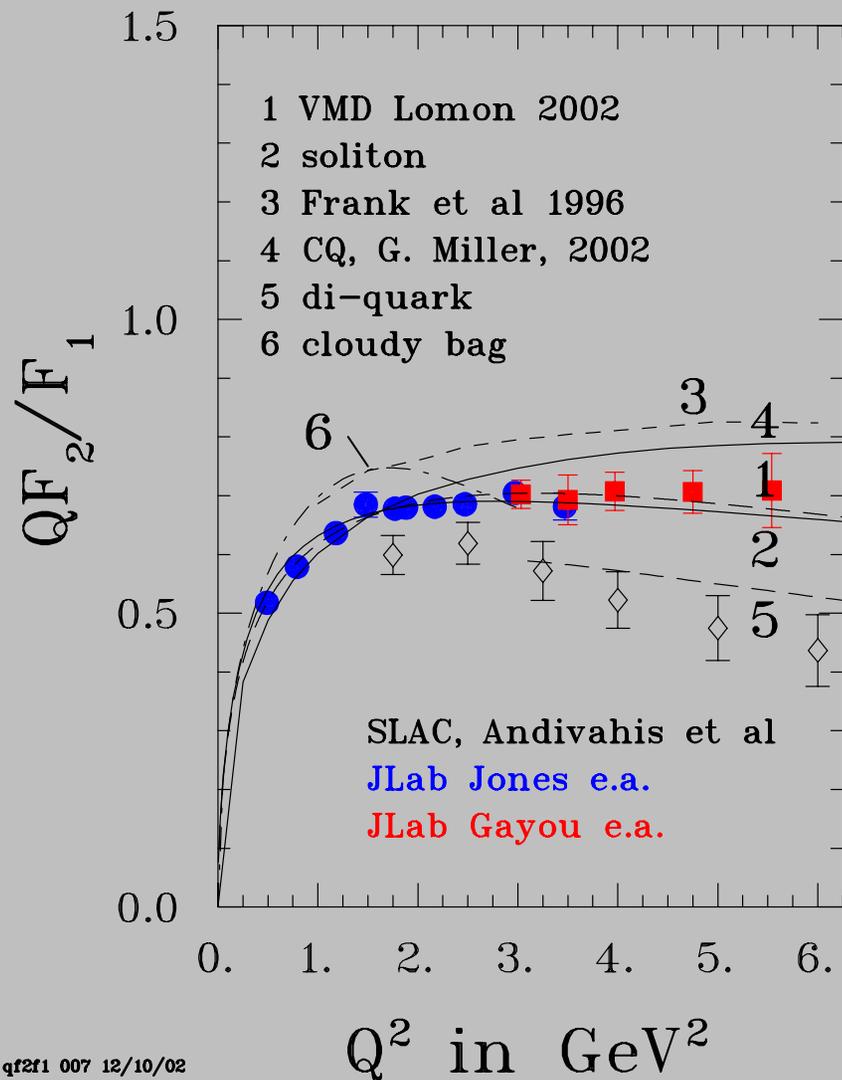
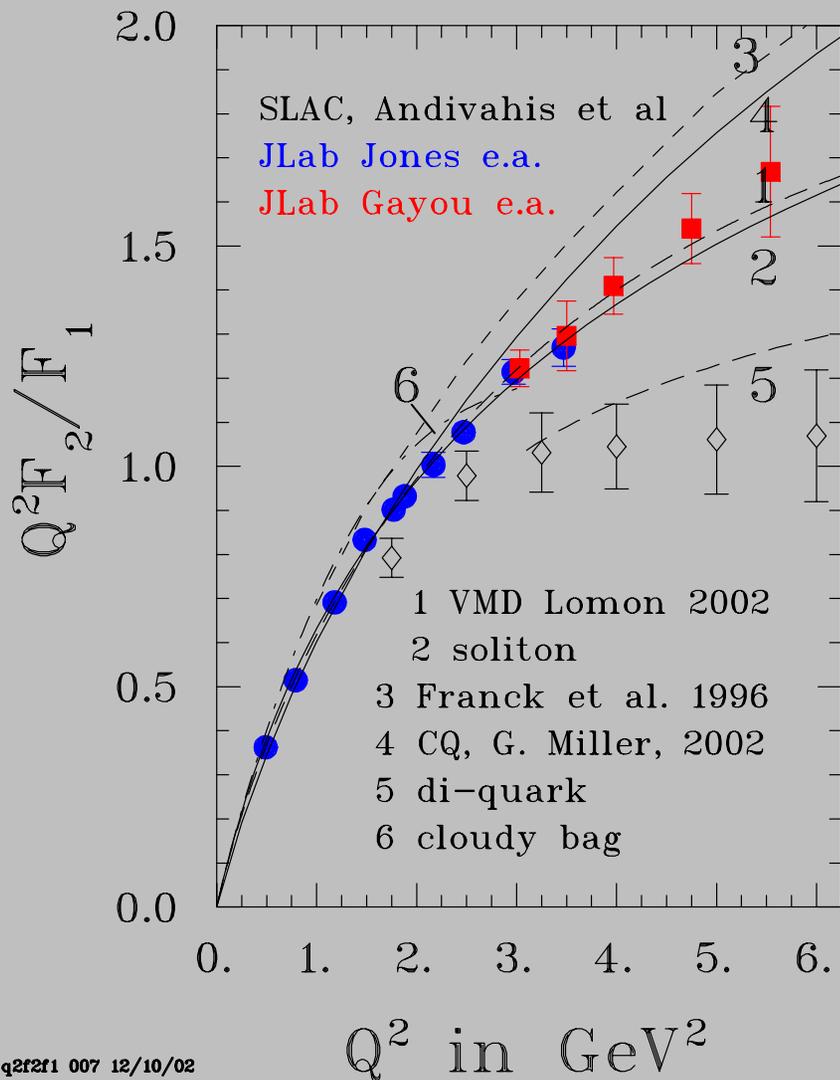
- VMD + pQCD (Lomon 2002)
- PFSA CQM GBE
- - - Soliton (Holzwarth b1)
- - - LF CQM qFF (Cardarelli)
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- LF CQM  $\pi$  (Miller)



# Proton Electric Form Factor



# Proton Electric Form Factor



old QCD prediction

new QCD prediction

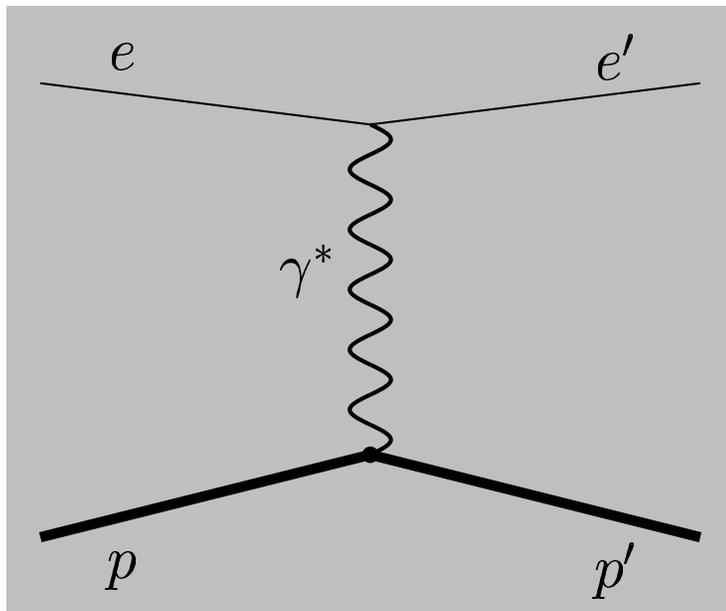
**Difference: quarks carry angular momentum**

# Proton Electric Form Factor

⇒ Why did cross section data not see this trend?

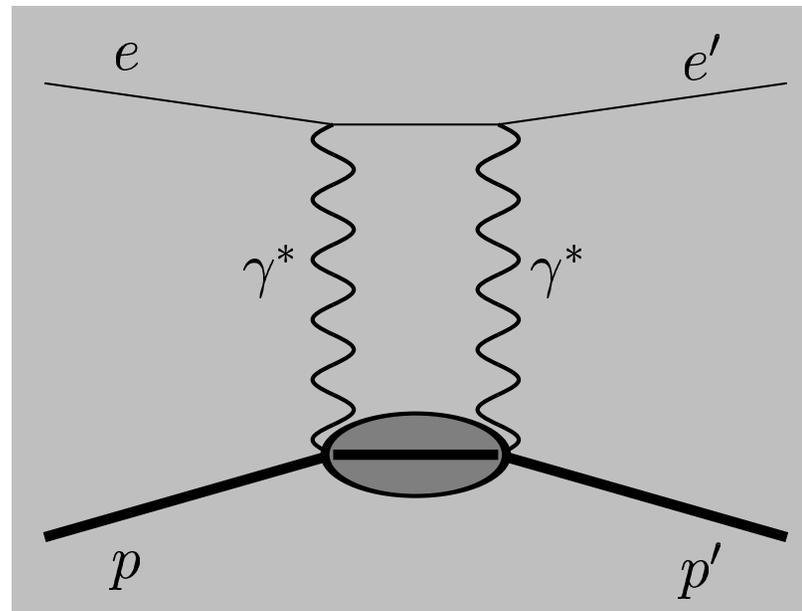
Currently Favored Theory:

1 $\gamma$ -Exchange



Born Approximation

2 $\gamma$ -Exchange



Elastic or Inelastic?

# Two Photon Exchange

In general:

$$T = \frac{e^2}{Q^2} \bar{u}(k') \gamma_\mu u(k) \bar{u}(p') \left[ \tilde{G}_M \gamma^\mu - \tilde{F}_2 \frac{P^\mu}{M} + \tilde{F}_3 \frac{\gamma \cdot K P^\mu}{M^2} \right] u(p)$$

Separating 1-photon and multi-photon contributions:

$$\tilde{G}_M(\epsilon, Q^2) = G_M(Q^2) + \delta \tilde{G}_M(\epsilon, Q^2)$$

$$\tilde{G}_E(\epsilon, Q^2) = G_E(Q^2) + \delta \tilde{G}_E(\epsilon, Q^2)$$

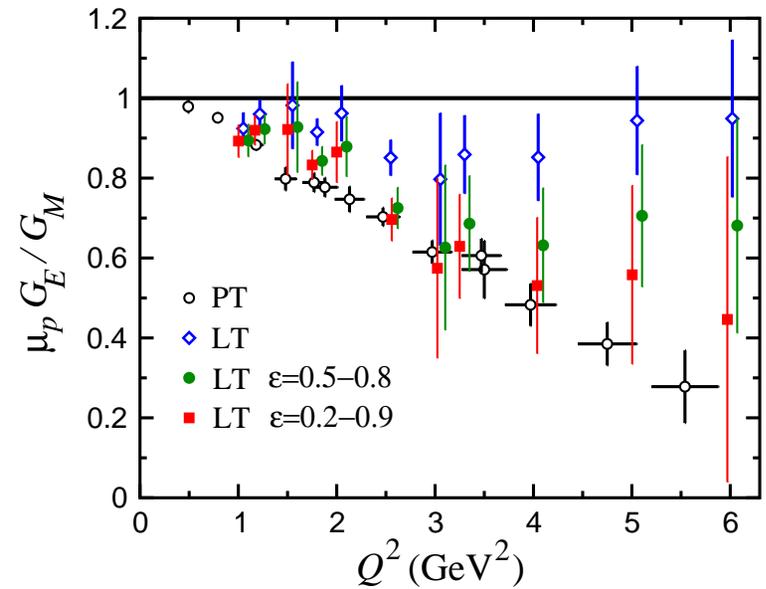
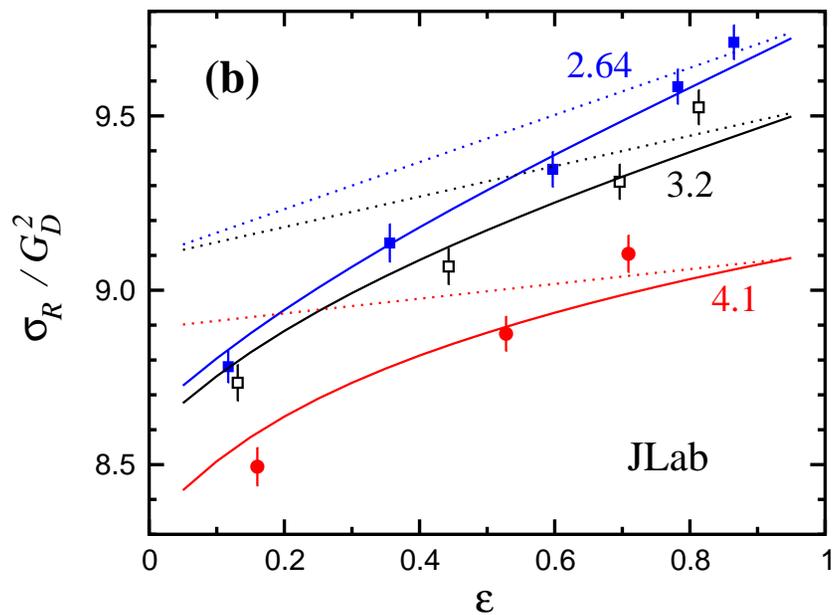
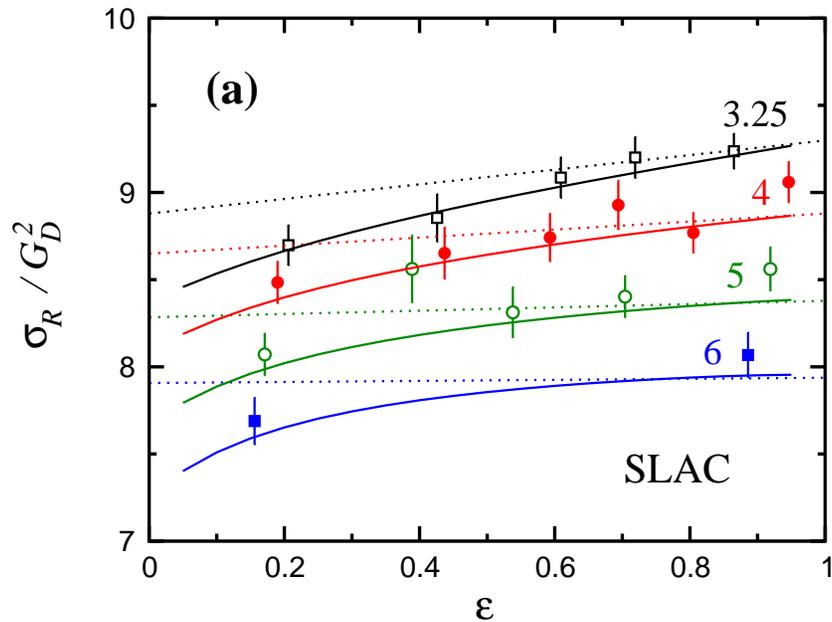
$$\tilde{F}_3(\epsilon, Q^2) = \delta \tilde{F}_3(\epsilon, Q^2)$$

with  $\tilde{G}_E = \tilde{G}_M - (1 + \tau) \tilde{F}_2$  and  $\frac{d\sigma}{d\Omega} = \sigma_{\text{Mott}} \times \frac{\tau}{\epsilon(1 + \tau)} \times \sigma_R$

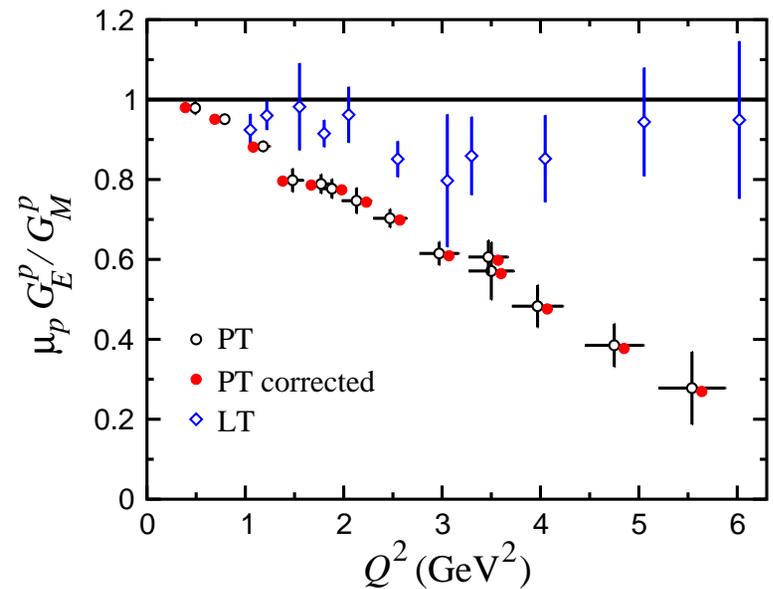
we obtain for 2-photon exchange:

$$\sigma_R = G_M^2 + \frac{\epsilon}{\tau} G_E^2 + 2G_M \mathcal{R}(\delta \tilde{G}_M + \frac{\epsilon \nu}{M^2} \tilde{F}_3) + 2\frac{\epsilon}{\tau} G_E \mathcal{R}(\delta \tilde{G}_E + \frac{\nu}{M^2} \tilde{F}_3)$$

# Impact of Two Photon Exchange



Phys. Rev. C 72, 034612 (2005)



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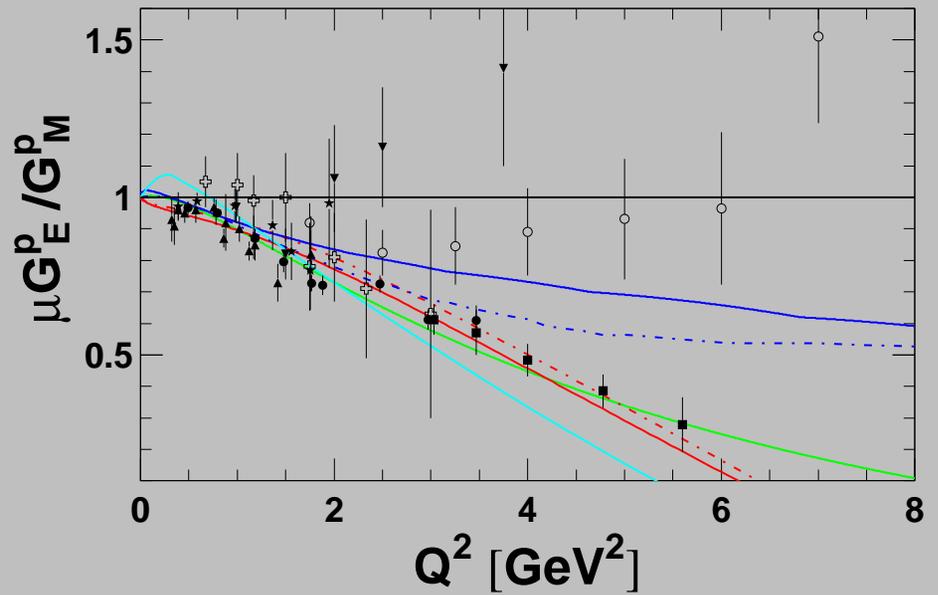
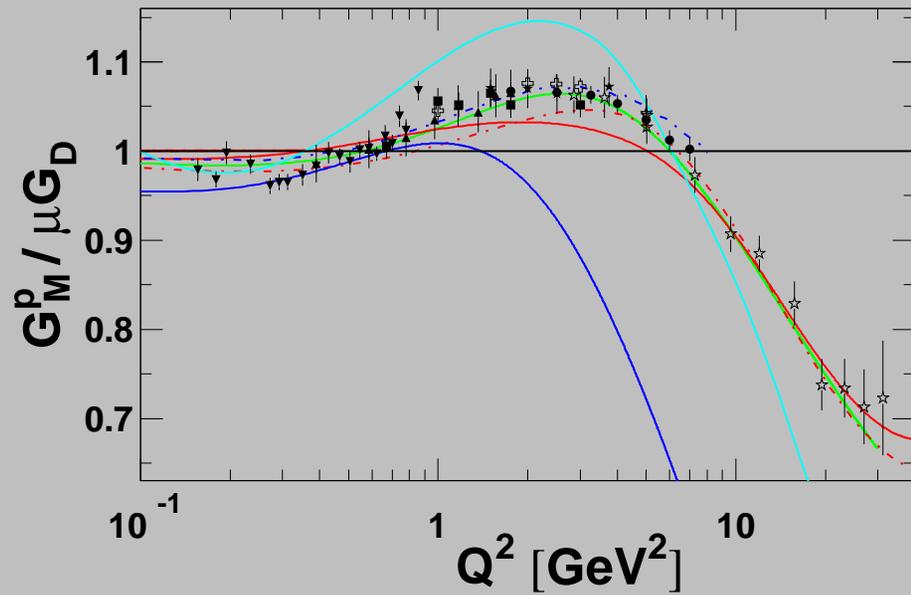
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- ▷ Techniques
- ▷ Limitations

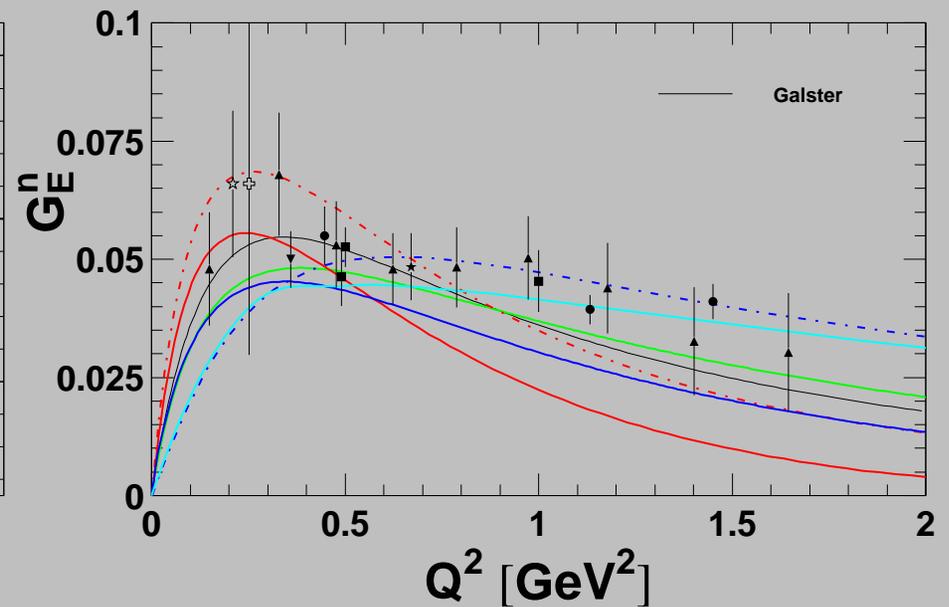
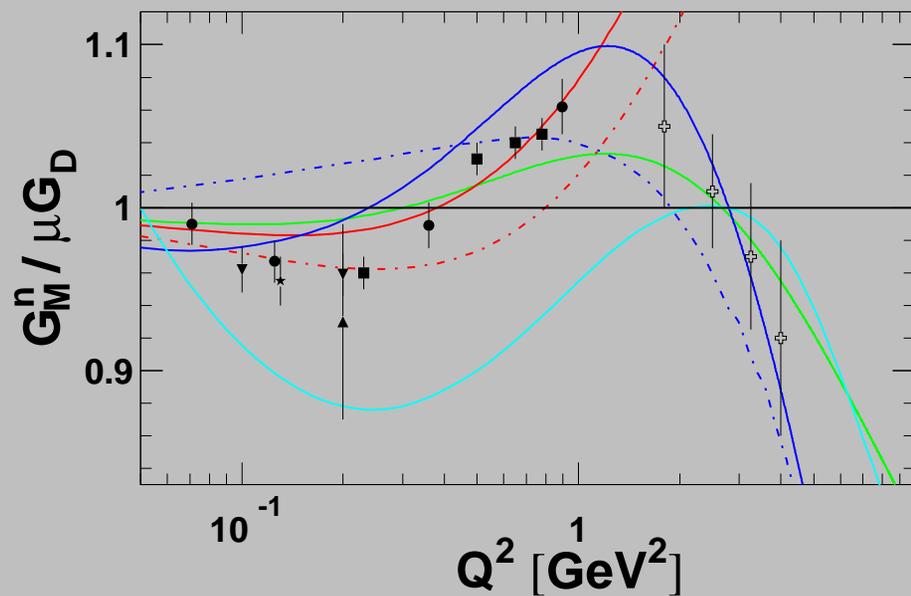
## *Theory Models*

## *Measurements at JLab*



— VMD + pQCD (Lomon 2002)  
- - - Soliton (Holzwarth b1)  
— Soliton (Holzwarth b2)

— PFSA CQM GBE  
- - - LF CQM qFF (Cardarelli)  
— LF CQM  $\pi$  (Miller)



# Relevant Form Factor Models

## ● PFSA CQM GBE

Eur. Phys. J. A 14, 17 (2002)

- *point-form spectator approximation*
- *quark–quark interaction fitted to spectroscopic data*
- *Goldstone boson exchange in impulse approximation with point-like constituent quarks*

## ● LF CQM qFF (Cardarelli)

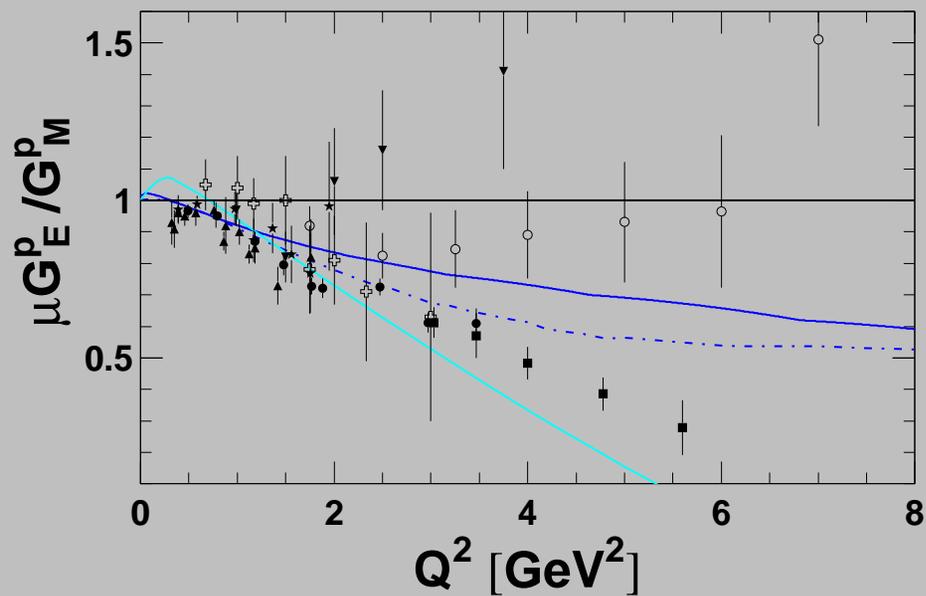
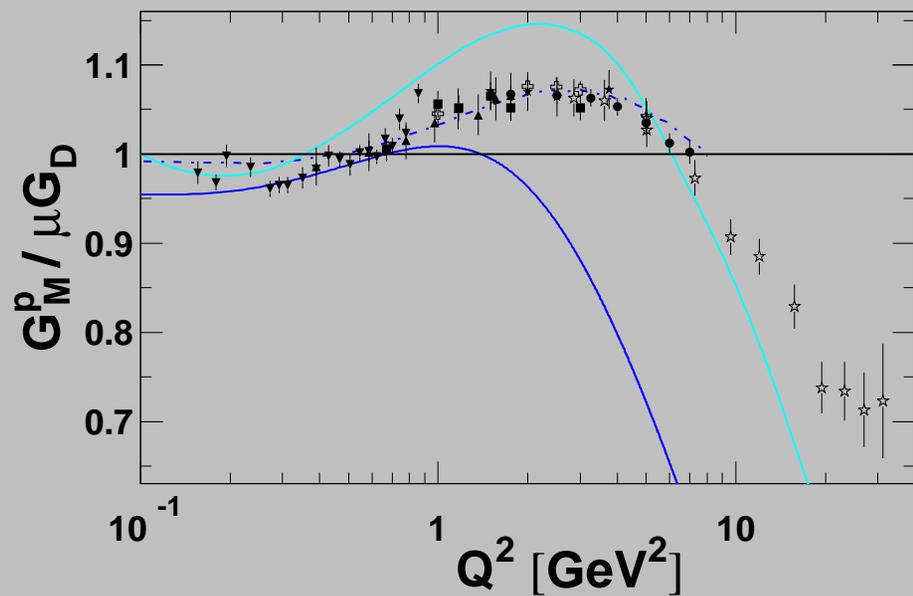
Phys. Rev. C 62, 065201 (2000)

- *1-gluon exchange light-front calculation*
- *quark–quark interaction fitted to spectroscopic data*
- *constituent quark FFs fitted to data  $Q^2 < 1$*
- *accounts only for 65% of neutron charge radius*

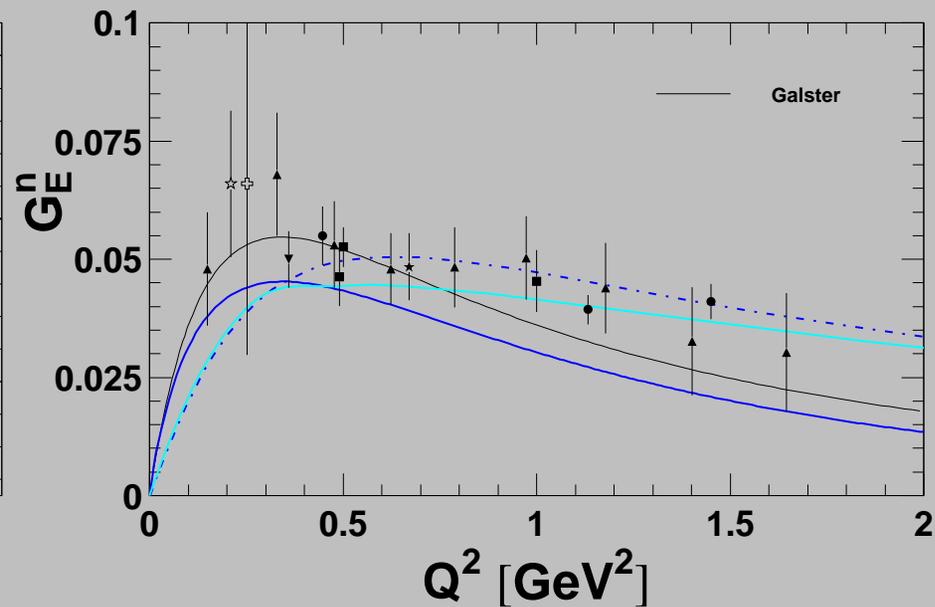
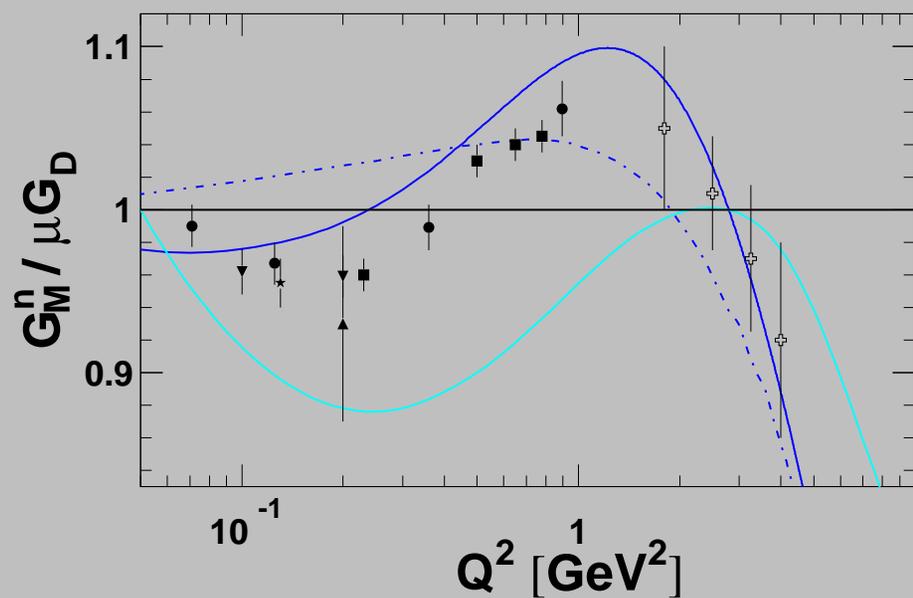
## ● LF CQM $\pi$ (Miller)

Phys. Rev. C 66, 032201(R) (2002)

- *3 point-like bound quarks surrounded by pion cloud*

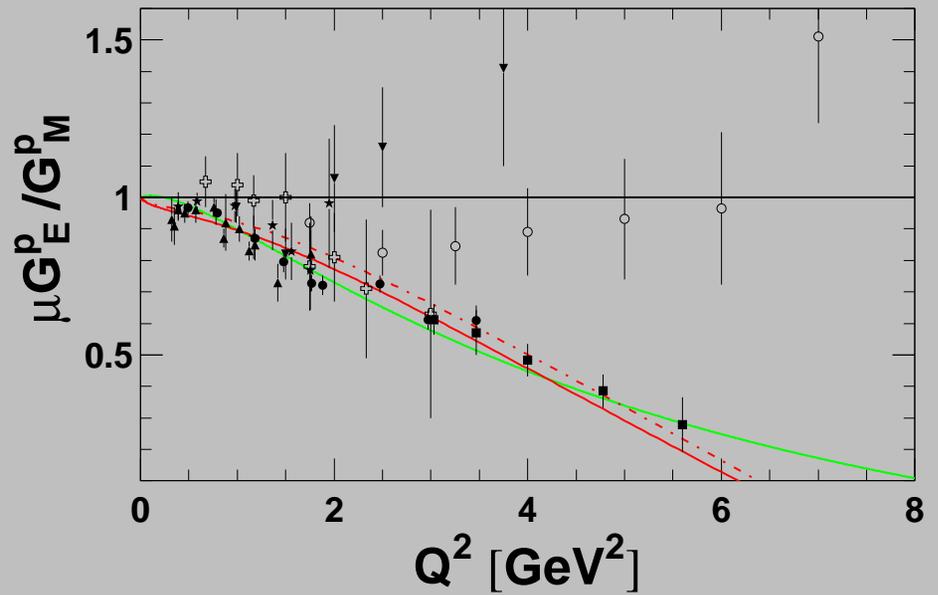
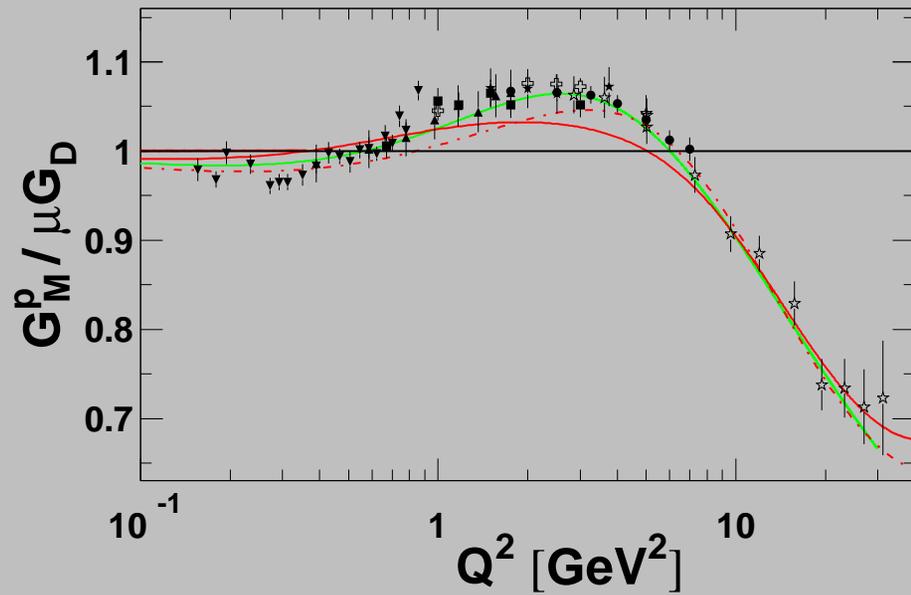


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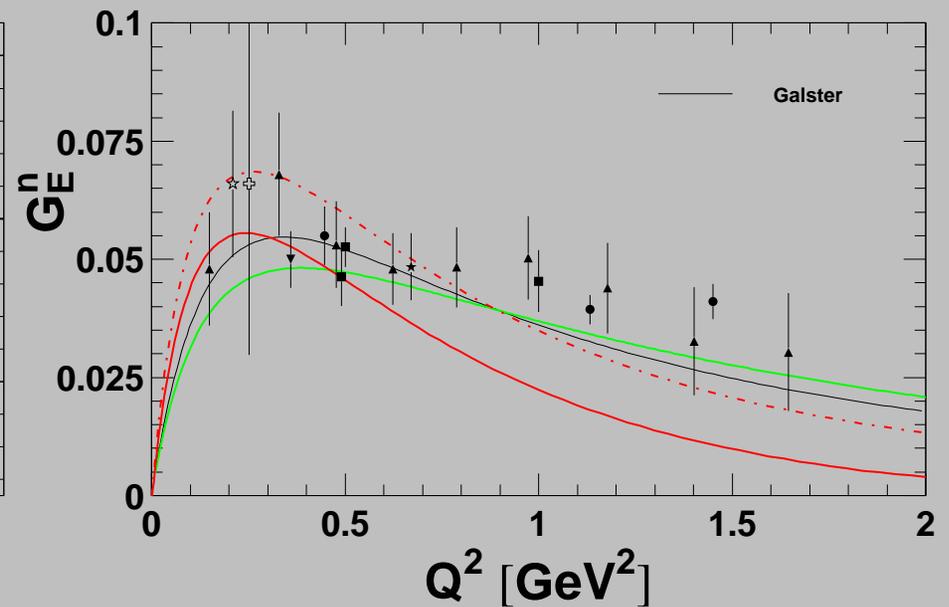
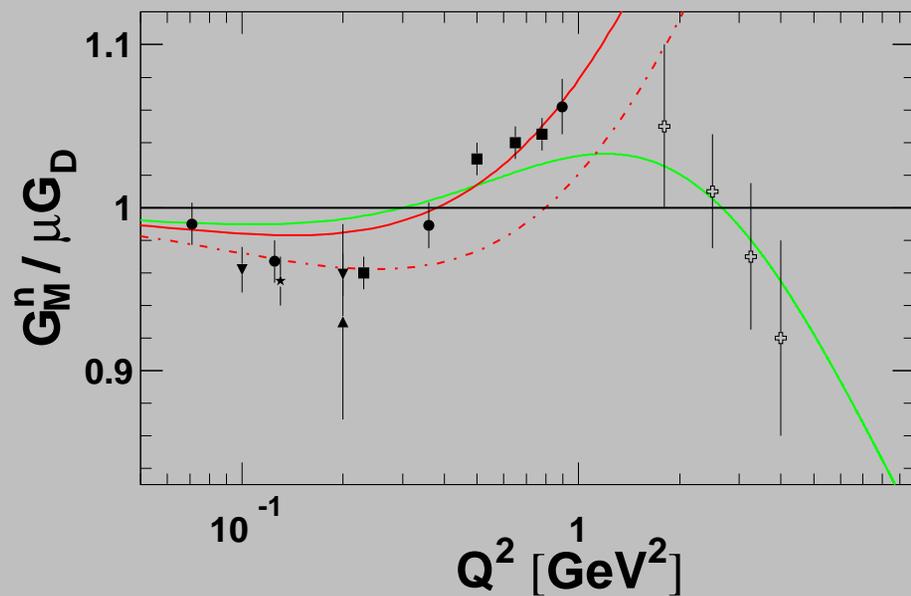


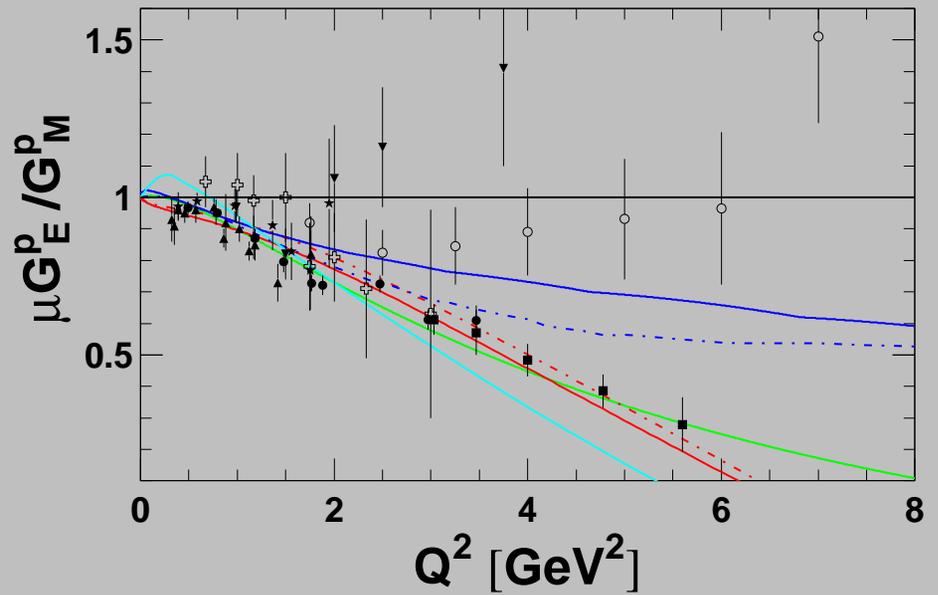
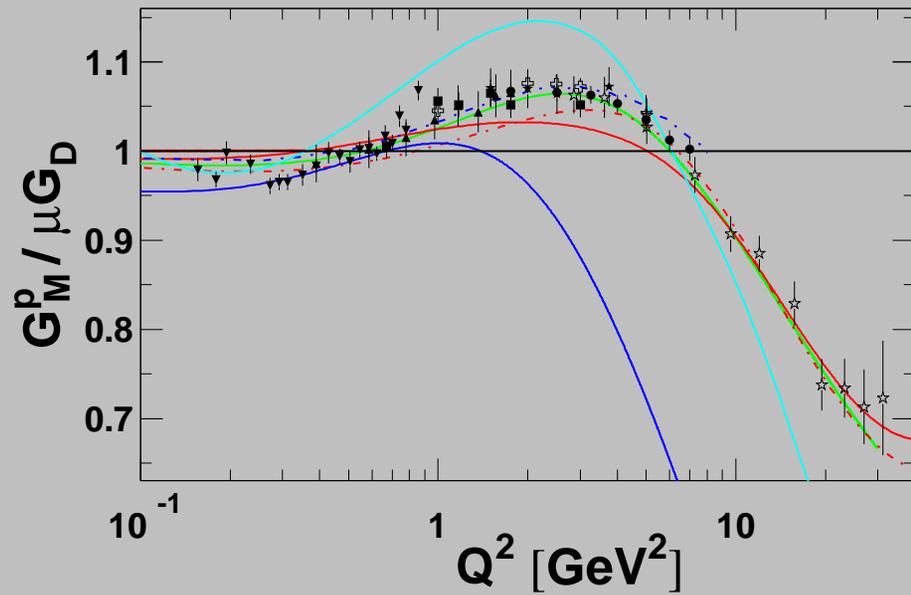
# Relevant Form Factor Models

- Soliton (Holzwarth) Z. Phys. A 356, 339 (1996)
  - *chiral soliton model, extended object*
  - *partial coupling to vector mesons*
  - *relativistic recoil corrections*
- VMD + pQCD (Lomon) Phys. Rev. C 66, 045501 (2002)
  - *interpolates low  $Q^2$  vector-meson dominance & high  $Q^2$  perturbative QCD*
  - *14 parameter fit*
  - *latest version of traditional meson-baryon approach*



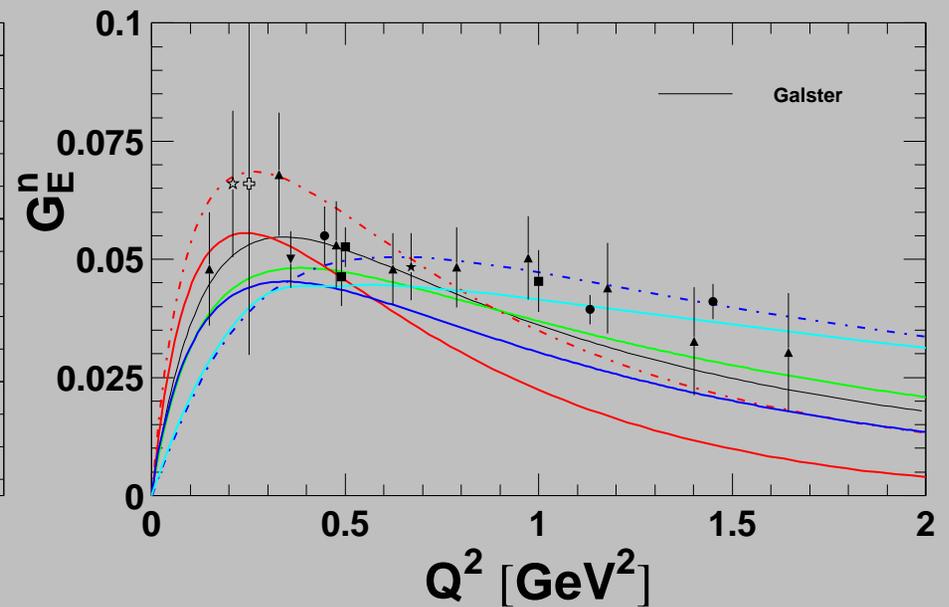
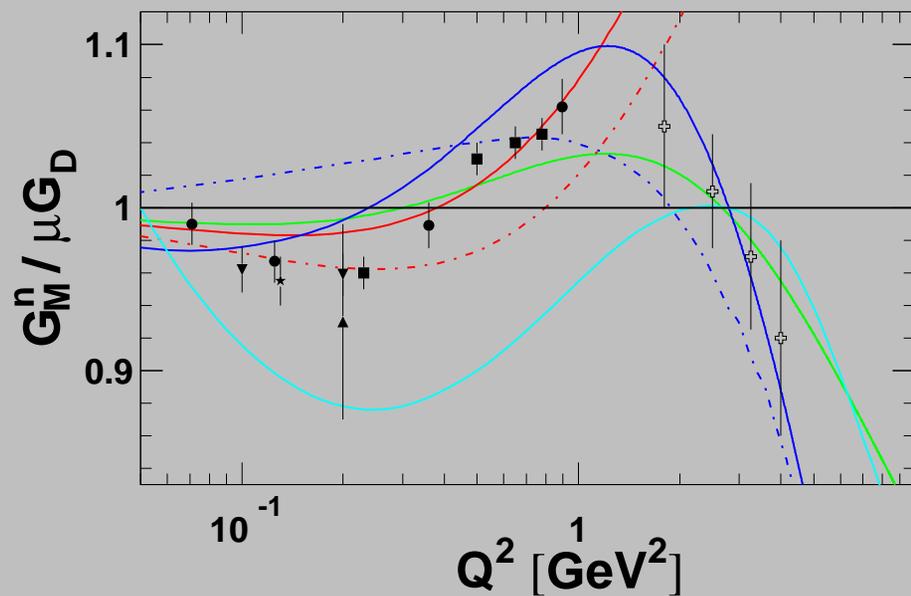
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— Soliton (Holzwarth b2)

— PFSA CQM GBE  
- - - LF CQM qFF (Cardarelli)  
— LF CQM  $\pi$  (Miller)



# *Nucleon Form Factors*

## *Introduction*

- ▷ Definition
- ▷ Formalism
- ▷ Interpretation & Utility

## *Data*

- ▷ Early Results
- ▷ Current Status

## *Measurements*

- ▷ Techniques
- ▷ Limitations

## *Theory Models*

## *Measurements at JLab*

# Form Factor Measurements at JLab

Proposal, Hall	Form Factor	Technique, Reaction	Year
93-026 C	$G_E^n$	Asymmetry $\vec{D}(\vec{e}, e'n)p$	1998,2001
93-027 A	$G_E^p/G_M^p$	Recoil ${}^1\text{H}(\vec{e}, e'\vec{p})$	1998
93-038 C	$G_E^n/G_M^n$	Recoil ${}^2\text{H}(\vec{e}, e'\vec{n})p$	2000/2001
94-017 B	$G_M^n$	Ratio $\frac{d(e,e'n)p}{d(e,e'p)n}$	2000
95-001 A	$G_M^n$	Asymmetry ${}^3\vec{\text{He}}(\vec{e}, e')X$	1999
99-007 A	$G_E^p/G_M^p$	Recoil ${}^1\text{H}(\vec{e}, e'\vec{p})$	2000
01-001 A	$G_E^p$	Rosenbluth ${}^1\text{H}(e, p)$	2002
02-013 A	$G_E^n$	Asymmetry ${}^3\vec{\text{He}}(\vec{e}, e'n)$	2006
04-108 C	$G_E^p/G_M^p$	Recoil ${}^1\text{H}(\vec{e}, e'\vec{p})$	2007

# Form Factor Measurements in Hall A

Proposal, Hall	Form Factor	Technique, Reaction	Year
93-026 C	$G_E^n$	Asymmetry $\vec{D}(\vec{e}, e'n)p$	1998,2001
93-027 A	$G_E^p/G_M^p$	Recoil ${}^1\text{H}(\vec{e}, e'\vec{p})$	1998
93-038 C	$G_E^n/G_M^n$	Recoil ${}^2\text{H}(\vec{e}, e'\vec{n})p$	2000/2001
94-017 B	$G_M^n$	Ratio $\frac{d(e,e'n)p}{d(e,e'p)n}$	2000
95-001 A	$G_M^n$	Asymmetry ${}^3\vec{\text{He}}(\vec{e}, e')X$	1999
99-007 A	$G_E^p/G_M^p$	Recoil ${}^1\text{H}(\vec{e}, e'\vec{p})$	2000
01-001 A	$G_E^p$	Rosenbluth ${}^1\text{H}(e, p)$	2002
02-013 A	$G_E^n$	Asymmetry ${}^3\vec{\text{He}}(\vec{e}, e'n)$	2006
04-108 C	$G_E^p/G_M^p$	Recoil ${}^1\text{H}(\vec{e}, e'\vec{p})$	2007

# Form Factor Measurements in Hall B

Proposal, Hall	Form Factor	Technique, Reaction	Year
93-026 C	$G_E^n$	Asymmetry $\vec{D}(\vec{e}, e'n)p$	1998,2001
93-027 A	$G_E^p/G_M^p$	Recoil ${}^1\text{H}(\vec{e}, e'\vec{p})$	1998
93-038 C	$G_E^n/G_M^n$	Recoil ${}^2\text{H}(\vec{e}, e'\vec{n})p$	2000/2001
94-017 B	$G_M^n$	Ratio $\frac{d(e,e'n)p}{d(e,e'p)n}$	2000
95-001 A	$G_M^n$	Asymmetry ${}^3\vec{\text{He}}(\vec{e}, e')X$	1999
99-007 A	$G_E^p/G_M^p$	Recoil ${}^1\text{H}(\vec{e}, e'\vec{p})$	2000
01-001 A	$G_E^p$	Rosenbluth ${}^1\text{H}(e, p)$	2002
02-013 A	$G_E^n$	Asymmetry ${}^3\vec{\text{He}}(\vec{e}, e'n)$	2006
04-108 C	$G_E^p/G_M^p$	Recoil ${}^1\text{H}(\vec{e}, e'\vec{p})$	2007

# Form Factor Measurements in Hall C

Proposal, Hall	Form Factor	Technique, Reaction	Year
93-026 C	$G_E^n$	Asymmetry $\vec{D}(\vec{e}, e'n)p$	1998,2001
93-027 A	$G_E^p/G_M^p$	Recoil ${}^1\text{H}(\vec{e}, e'\vec{p})$	1998
93-038 C	$G_E^n/G_M^n$	Recoil ${}^2\text{H}(\vec{e}, e'\vec{n})p$	2000/2001
94-017 B	$G_M^n$	Ratio $\frac{d(e, e'n)p}{d(e, e'p)n}$	2000
95-001 A	$G_M^n$	Asymmetry ${}^3\vec{\text{He}}(\vec{e}, e')X$	1999
99-007 A	$G_E^p/G_M^p$	Recoil ${}^1\text{H}(\vec{e}, e'\vec{p})$	2000
01-001 A	$G_E^p$	Rosenbluth ${}^1\text{H}(e, p)$	2002
02-013 A	$G_E^n$	Asymmetry ${}^3\vec{\text{He}}(\vec{e}, e'n)$	2006
04-108 C	$G_E^p/G_M^p$	Recoil ${}^1\text{H}(\vec{e}, e'\vec{p})$	2007

# Hall C Form Factor Measurements

## E 93-026

- *measured  $G_E^n$  from polarization asymmetry*
- *ran 1998 and 2001*
- *1998 measurement provided highest  $Q^2$  point at the time*

## E 93-038

- *measured  $G_E^n$  from recoil polarization*
- *ran 2000 through 2001*
- *currently most accurate measurement at large  $Q^2$*

## E 04-108

- *scheduled to run 2007*
- *will measure  $G_E^p/G_M^p$  through recoil polarization*
- *extension of spectacular Hall A results*

# Recall: Asymmetry Measurement

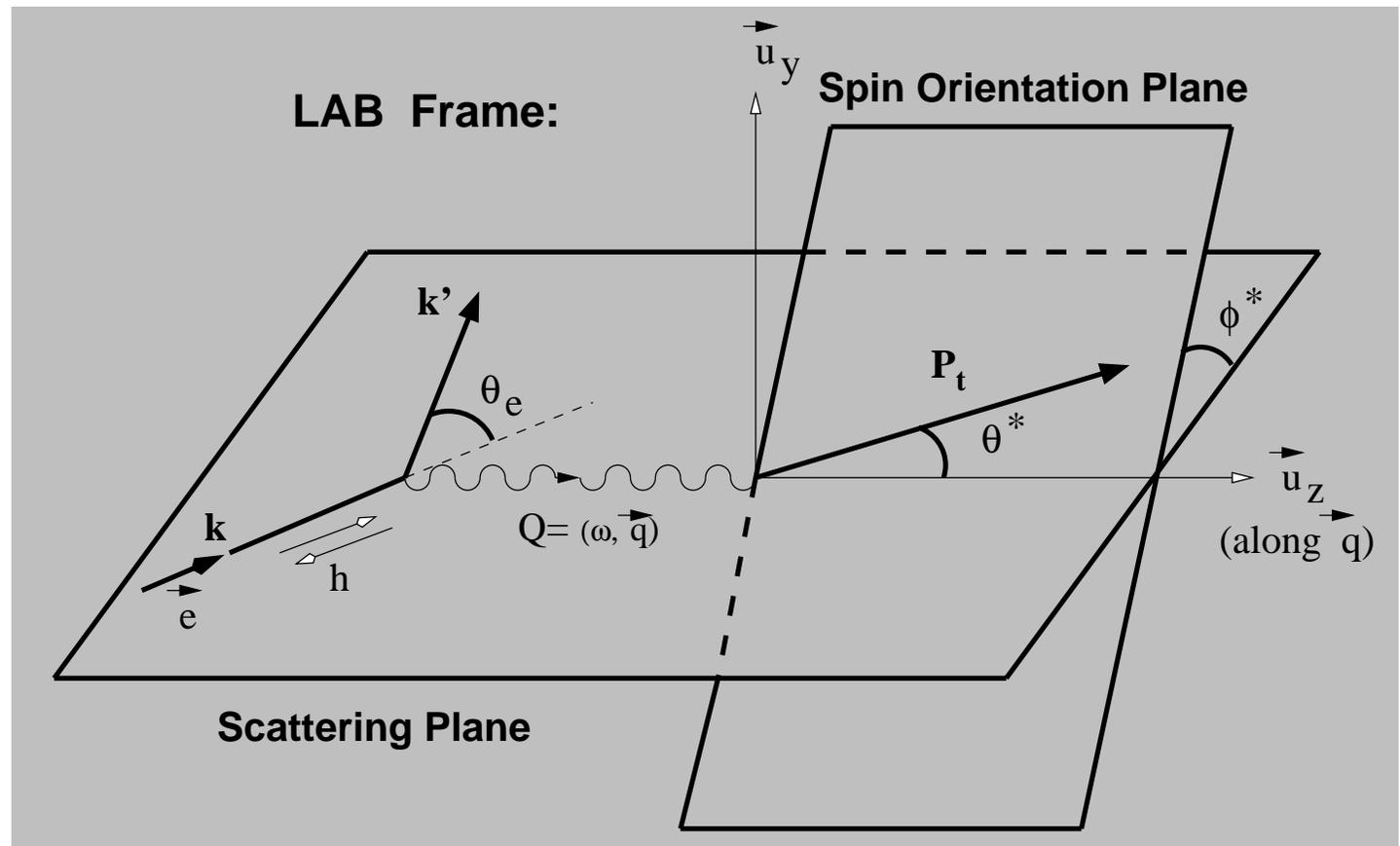
for quasi-free,

$$\mathcal{P}_{\text{target}} \perp \vec{q}$$

$$(\theta^* = 90^\circ)$$

and

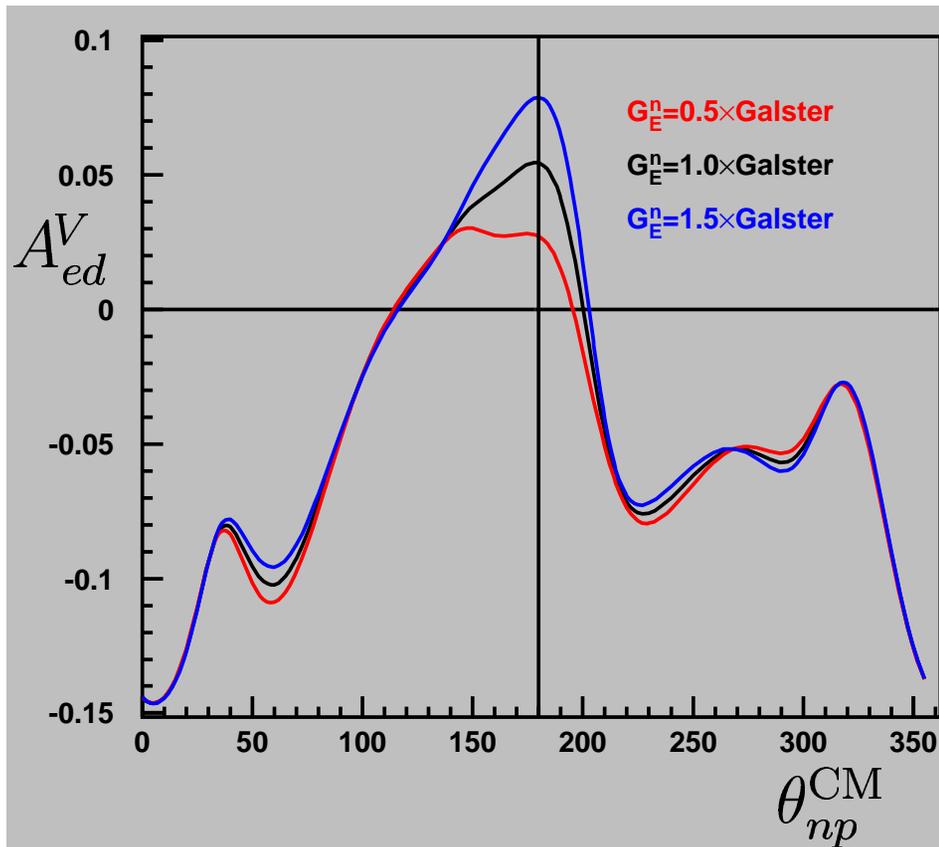
$\mathcal{P}_{\text{target}}$  in  
scattering plane  
( $\phi^* = 0$ ),



$$A^V = \frac{-2 \sqrt{\tau(1+\tau)} \tan \frac{\theta_e}{2} G_E G_M}{G_E^2 + \tau [1 + 2(1+\tau) \tan^2 \frac{\theta_e}{2}] G_M^2}$$

# $G_E^n$ Asymmetry – E93-026

E93-026 measured  $G_E^n$  via polarization asymmetry in quasi-elastic scattering off Deuterium



To extract measured  $G_E^n$ , compare:

measured  $A_{ed}^V$

and

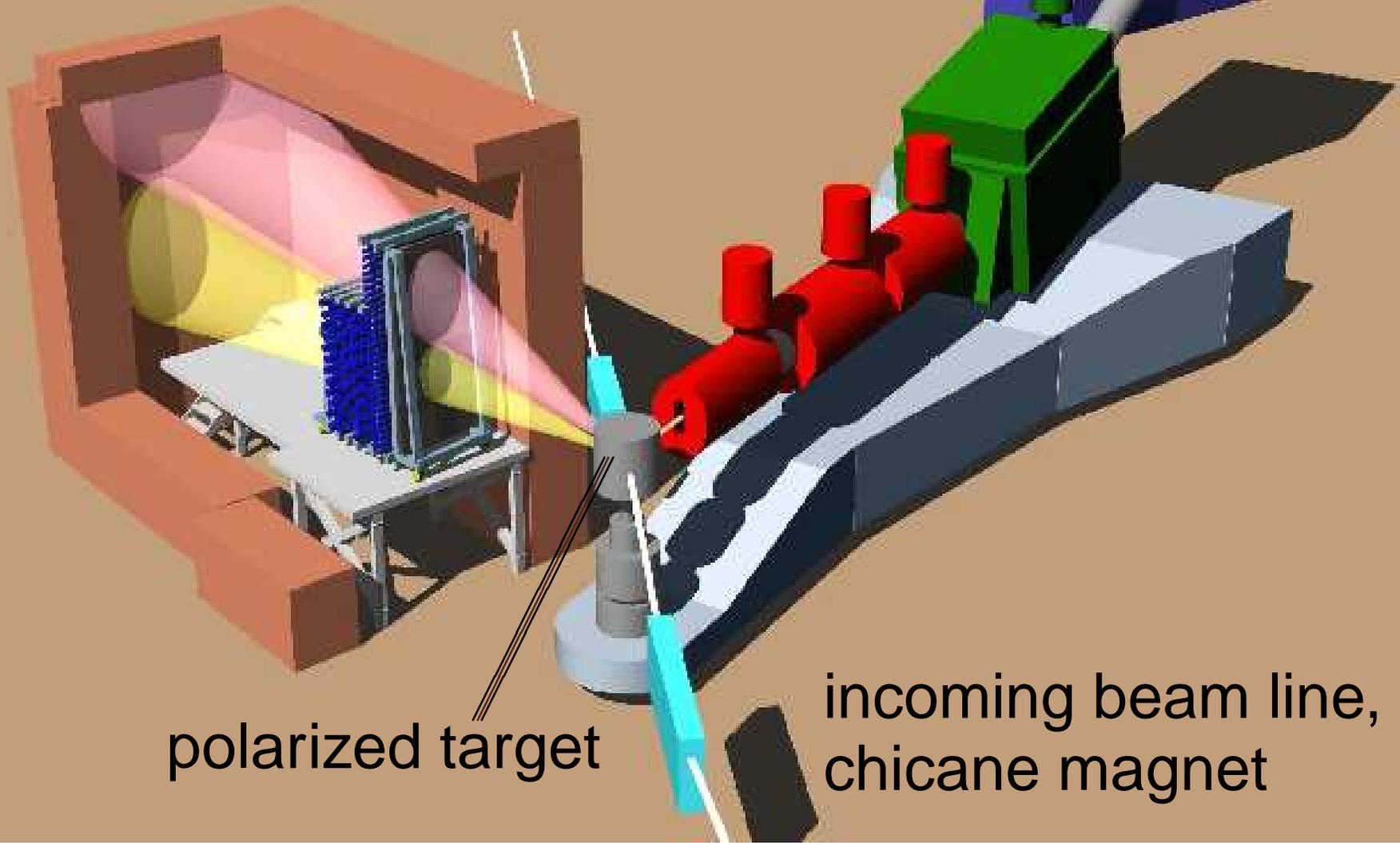
model calculations with different values of  $G_E^n$

Quasi-Elastic kinematics: In center of mass,  $\theta_{np} = 180^\circ$

Gen01

neutron detector

High  
Momentum  
Spectrometer

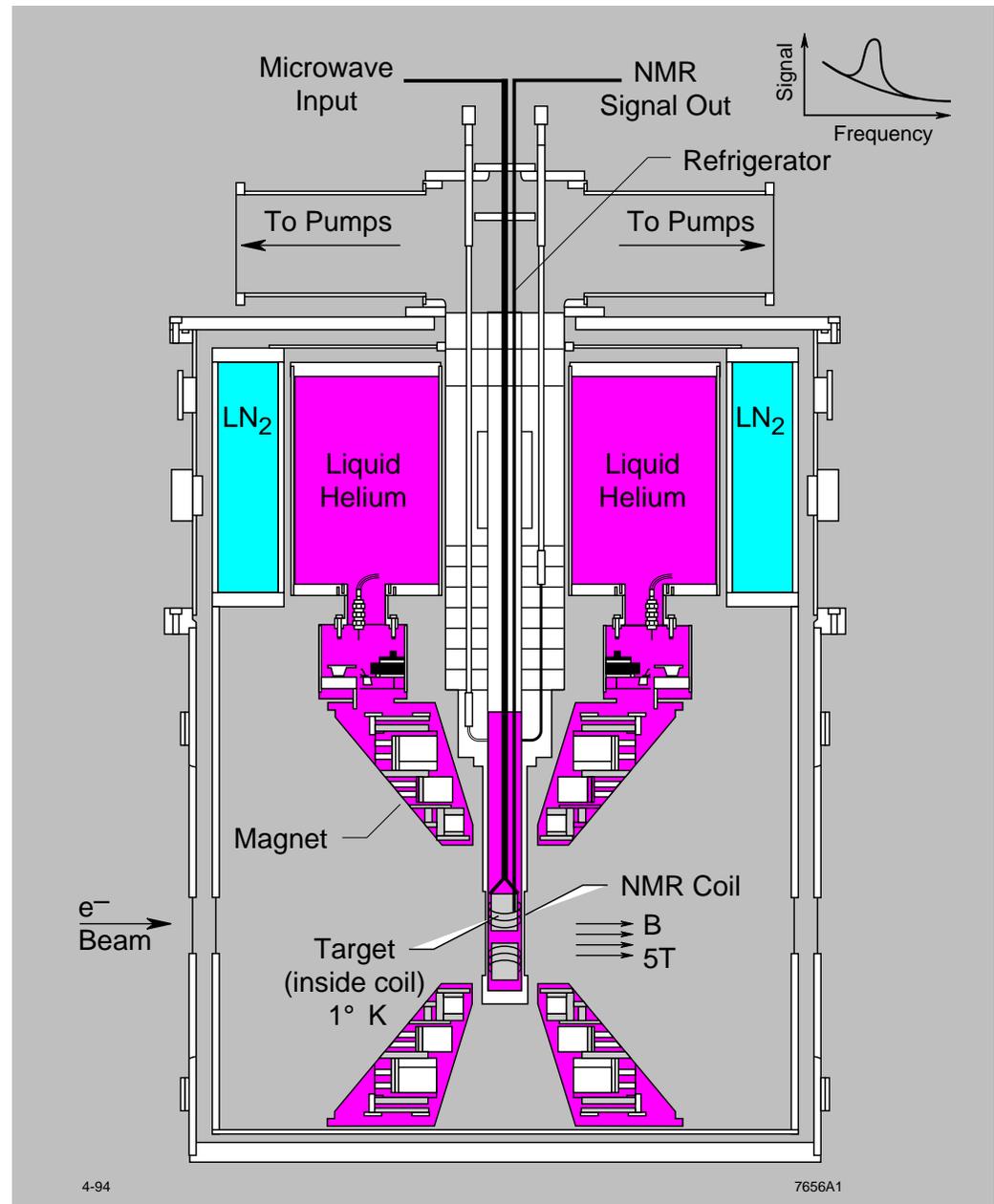


polarized target

incoming beam line,  
chicane magnet

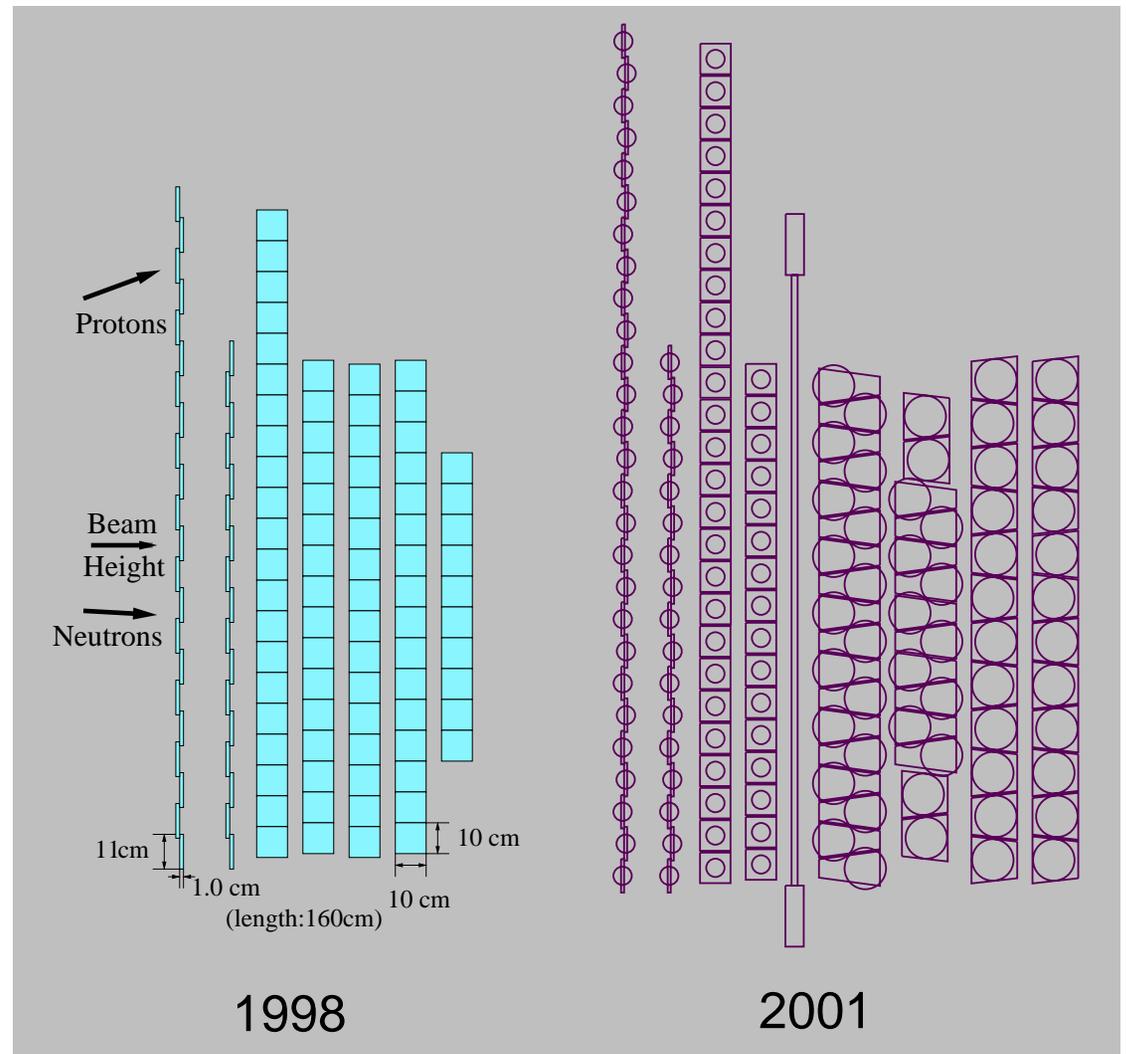
# Gen01 – Polarized Target

- frozen  $\text{ND}_3$
- $^4\text{He}$  evaporation refrigerator
- 5 T polarizing field
- dynamic nuclear polarization driven by microwaves
- NMR monitoring



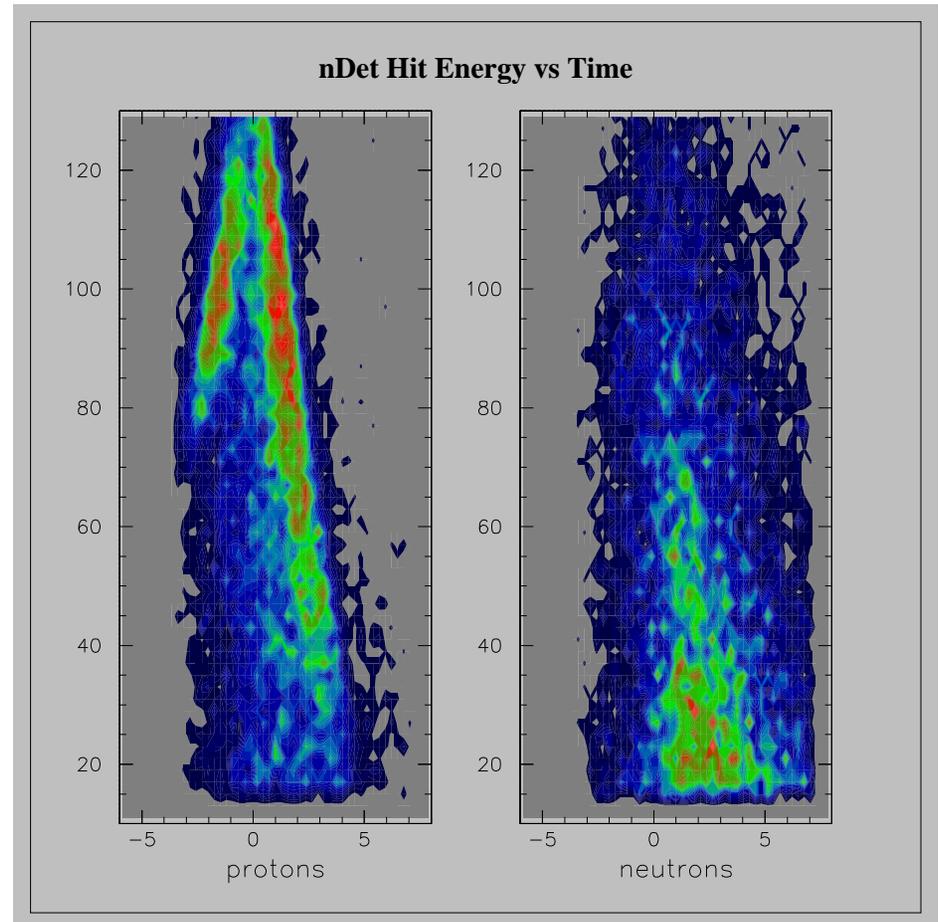
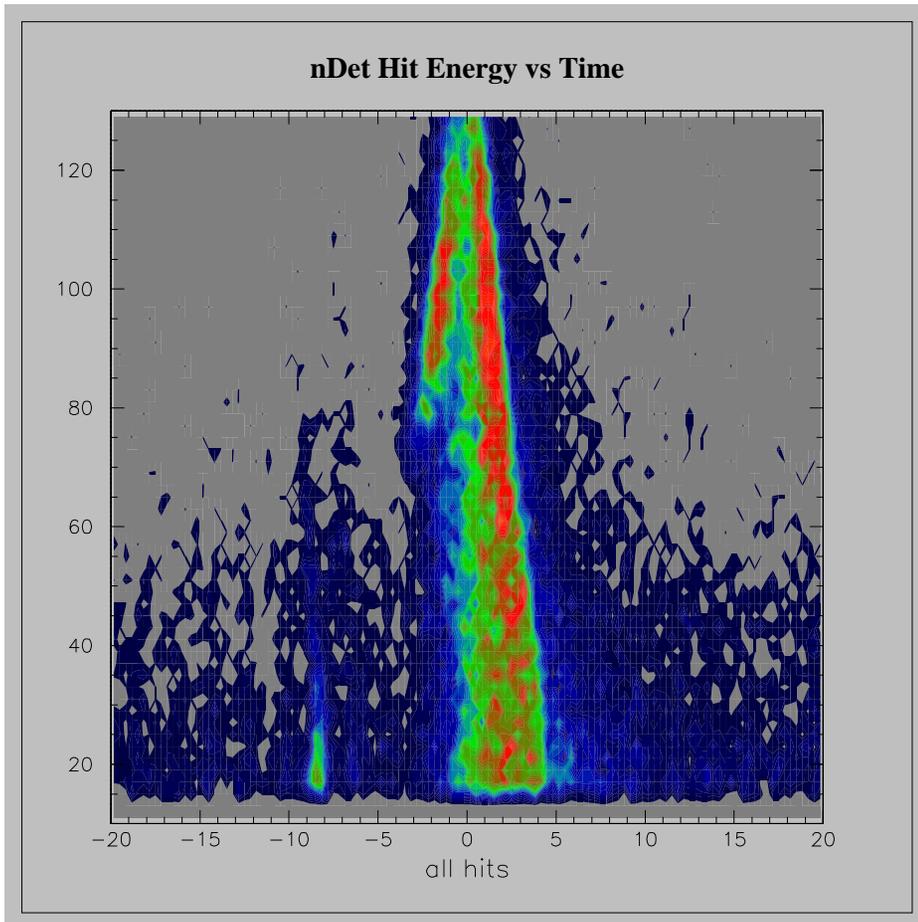
# Gen01 – Neutron Detector

- segmented scintillator
- $2 p^+$  VETO layers
- 6 conversion layers
- high rate:  $\sim 100 \text{ kHz}$
- vertically extended for symmetric proton acceptance
- provides 3 space coords, time & energy



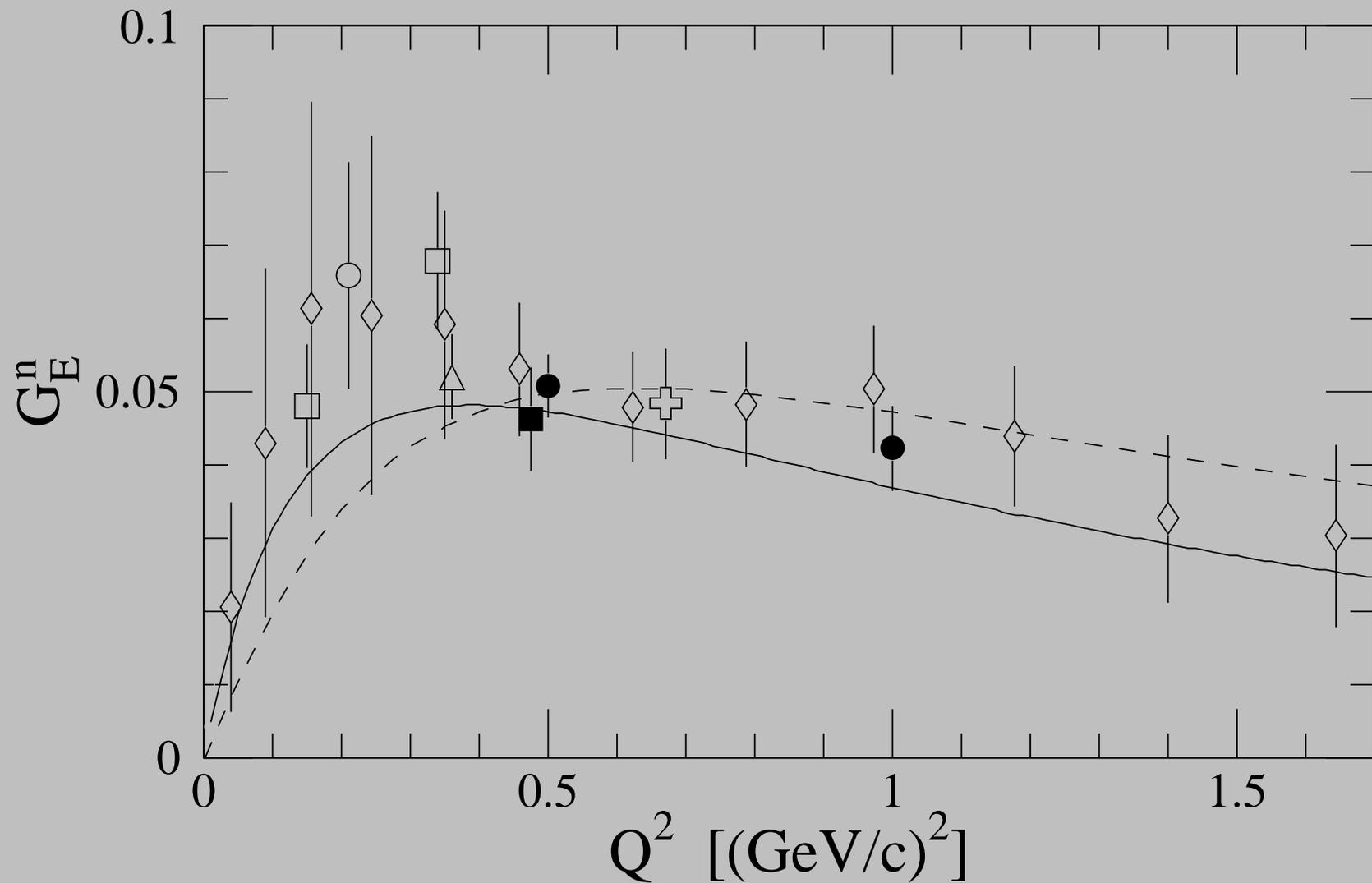
# Gen01 – Particle Identification

Particle Energy plotted against Detection Time



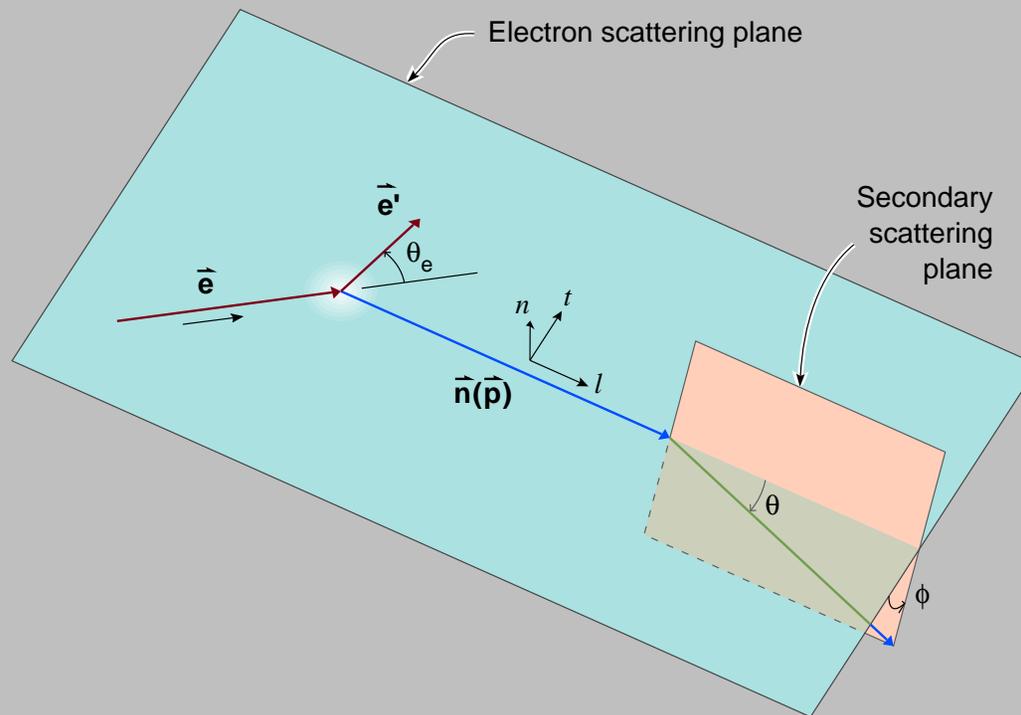
arbitrary offset; only hit times and VETO matches were considered

# Gen01 – Results



nucl-ex/0308021

# Recall: Recoil Polarimetry



$$I_0 P_n = 0$$

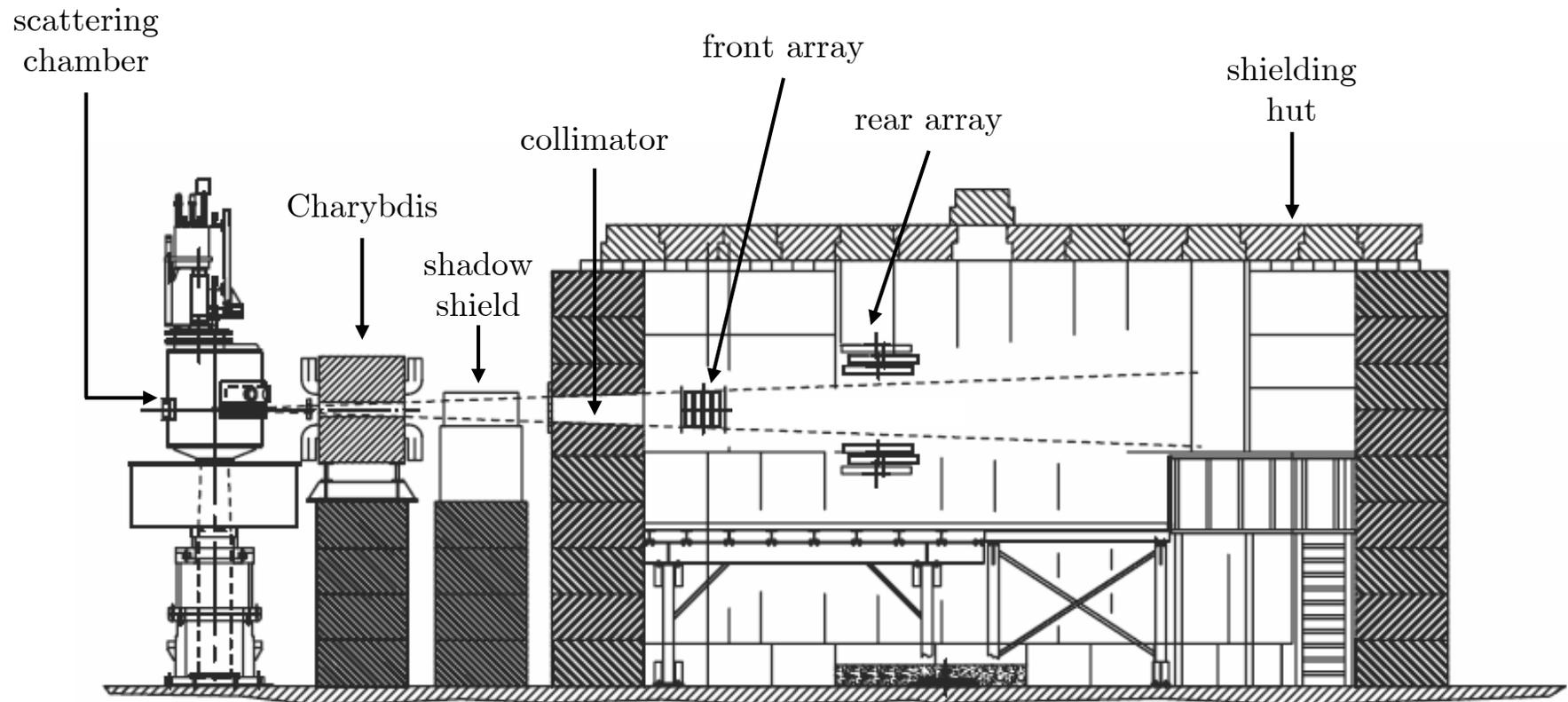
$$I_0 P_t = -2\sqrt{\tau(1+\tau)} G_E G_M \tan(\theta_e/2)$$

$$I_0 P_l = \frac{1}{M}(E_e + E_{e'})\sqrt{\tau(1+\tau)} G_M^2 \tan^2(\theta_e/2)$$

$$\frac{G_E}{G_M} = -\frac{P_t (E_e + E_{e'})}{P_l 2M} \tan\left(\frac{\theta_e}{2}\right)$$

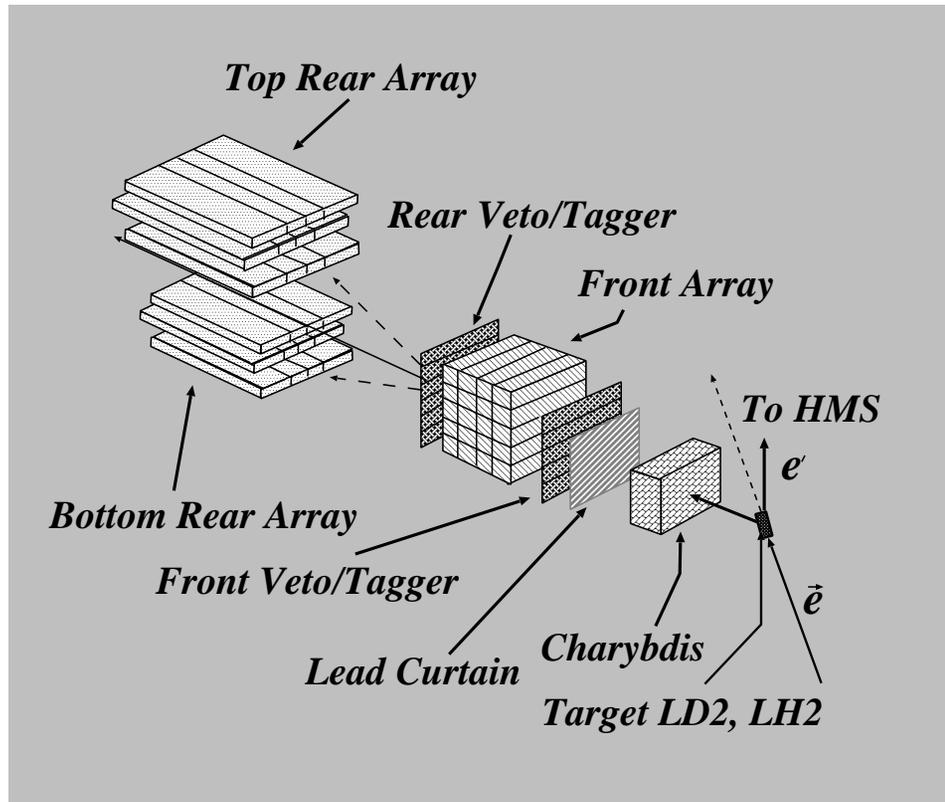
Direct measurement of form factor ratio by measuring the ratio of the transferred polarization  $P_t$  and  $P_l$

# $G_E^n$ Recoil Polarimetry – E93-038

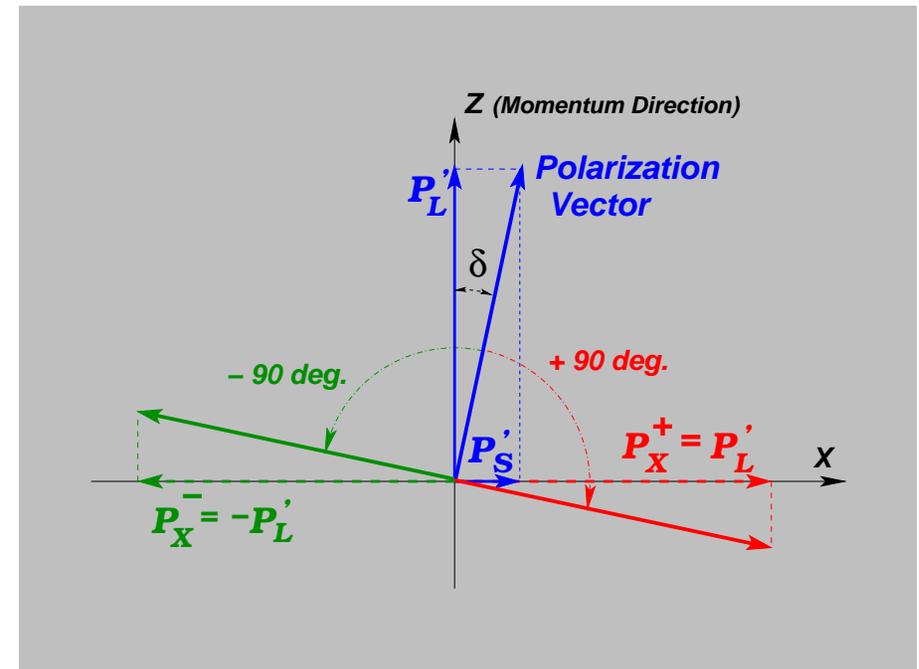


E93-038 measured  $G_E^n$  via recoil polarization in quasi-elastic scattering off Deuterium at  $Q^2 = 0.45, 1.13, \text{ and } 1.45 \text{ (GeV}/c)^2$  using the HMS in  ${}^2\text{H}(\vec{e}, e'\vec{n}){}^1\text{H}$  scattering

# E93-038 – Method



want to determine  $P_l$  and  $P_t$  at target  
polarimeter sensitive to transverse pol only



→ rotate longitudinal pol with *Charybdis* magnet

$$P_t^{\text{pol}} = P_l \sin \chi + P_t \cos \chi$$

# E93-038 – Data

## Coincidence VS Front-Rear TOF

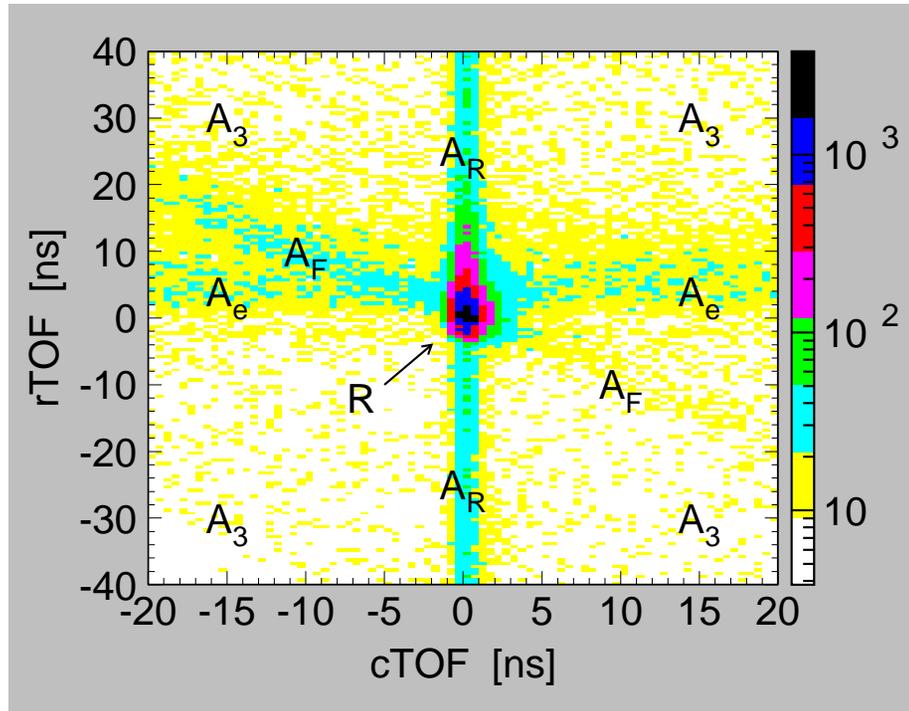
5 Distinct regions:

$A_3$  triple accidental,

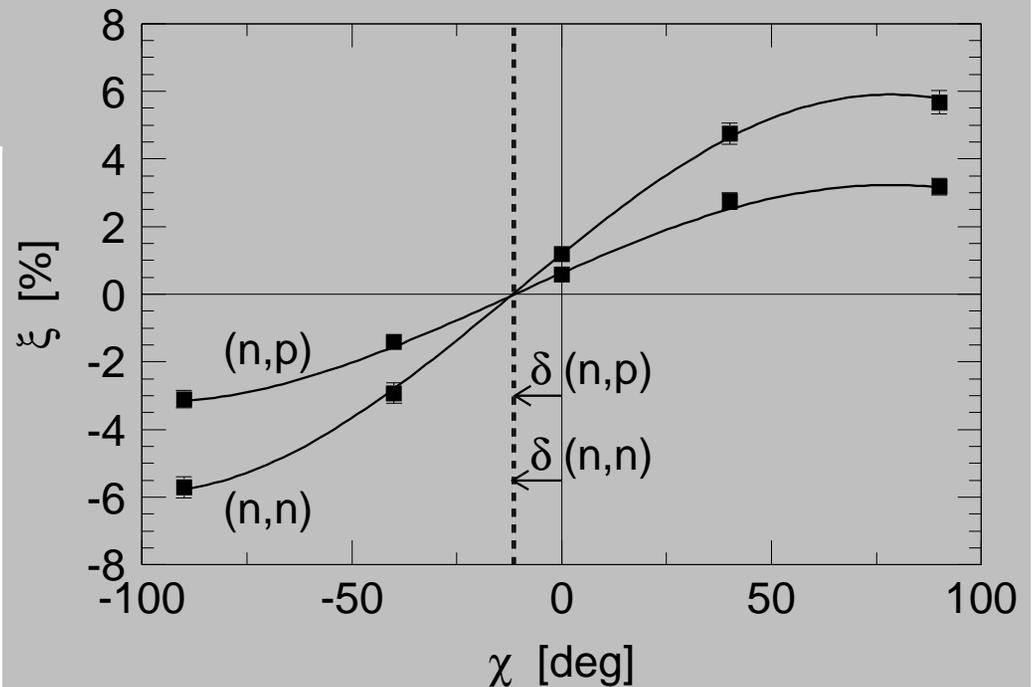
$A_e$  accidental  $e$ ,

$A_F/A_R$  accidental front/rear,

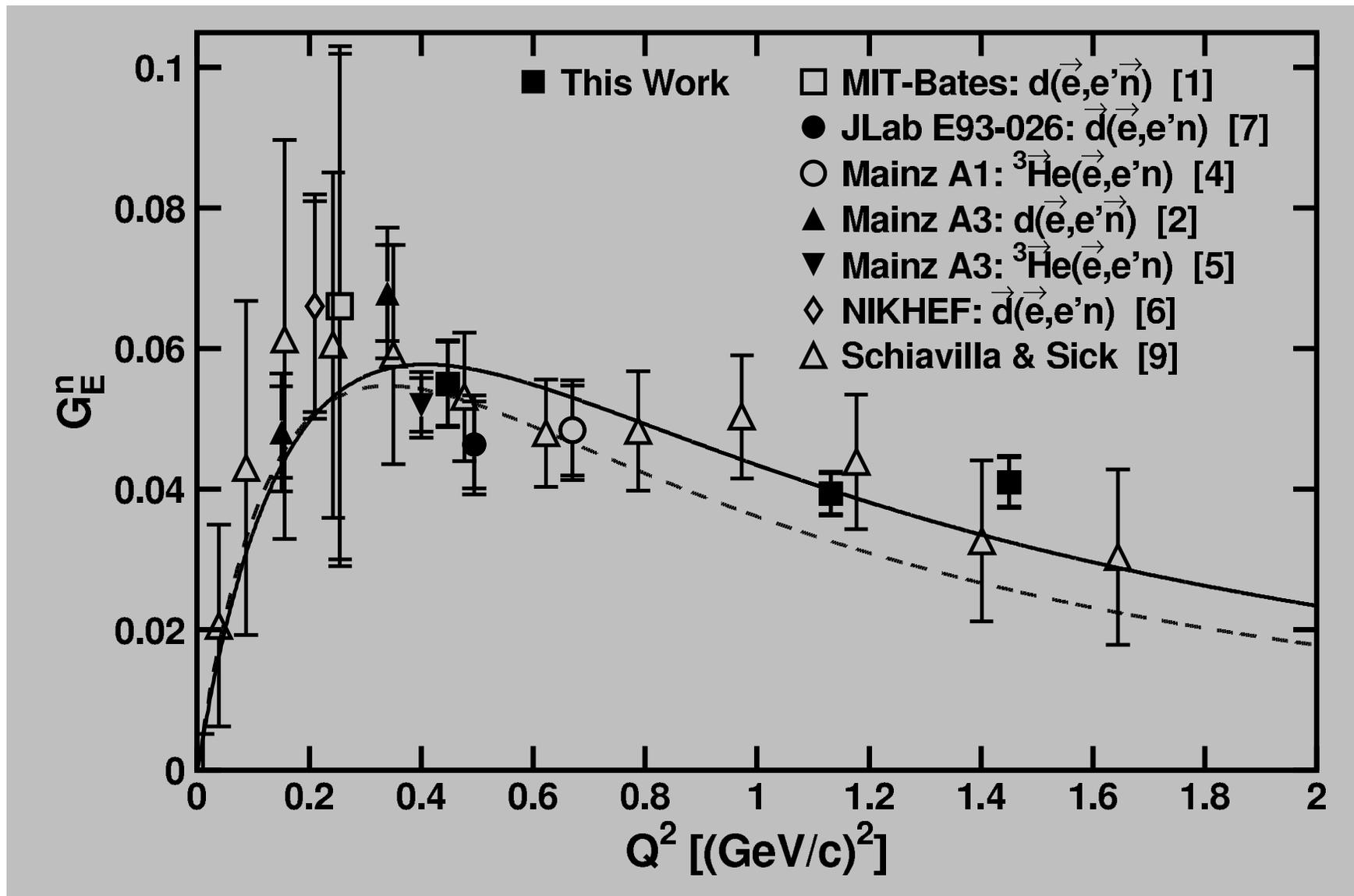
$R$  triple coincidence



Measured Asymmetry VS  
Precession Angle  
phase  $\delta$  correlates to  $G_E^n$

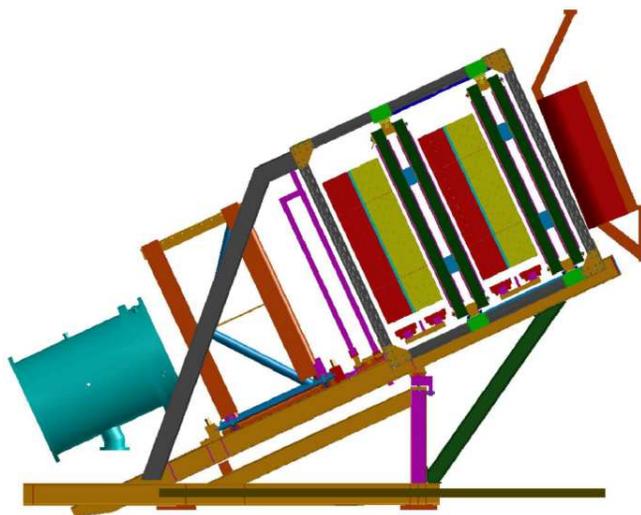
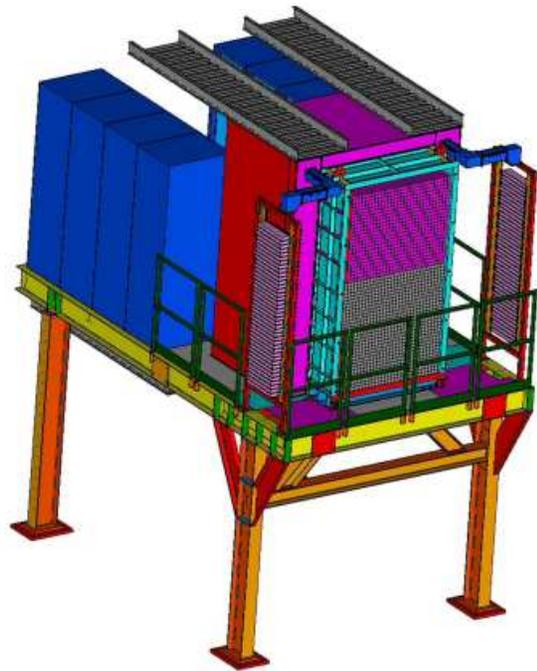


# E93-038 – Results

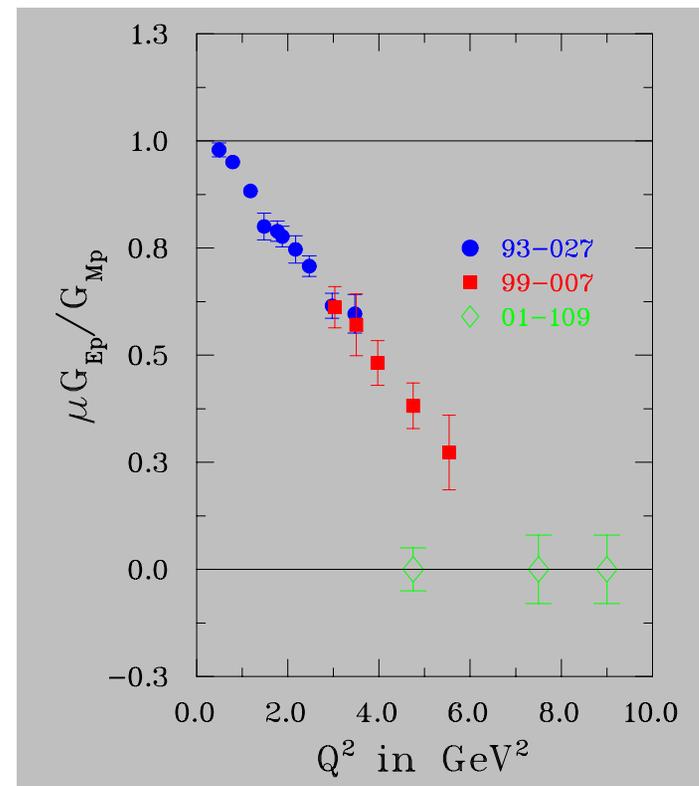


nucl-ex/0308007

# $G_E^p$ Recoil Polarimetry – E04-108



E04-108 will measure  $G_E^p/G_M^p$  at highest  $Q^2$  yet, using *new* calorimeter and polarimeter

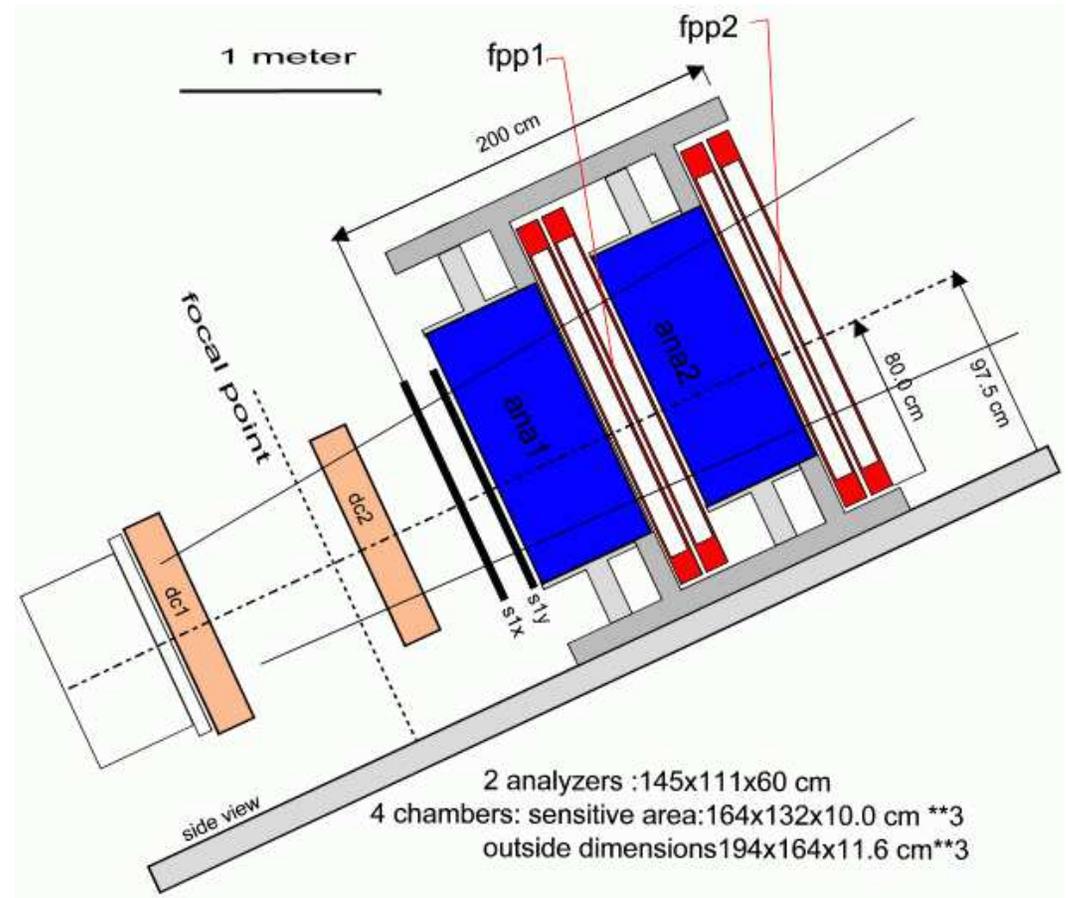
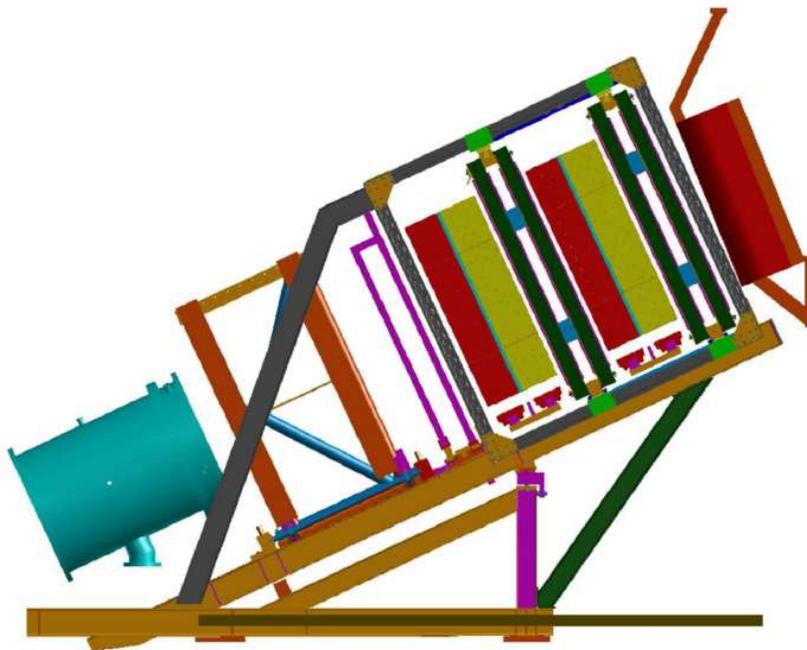


# *E04-108 – BigCal*



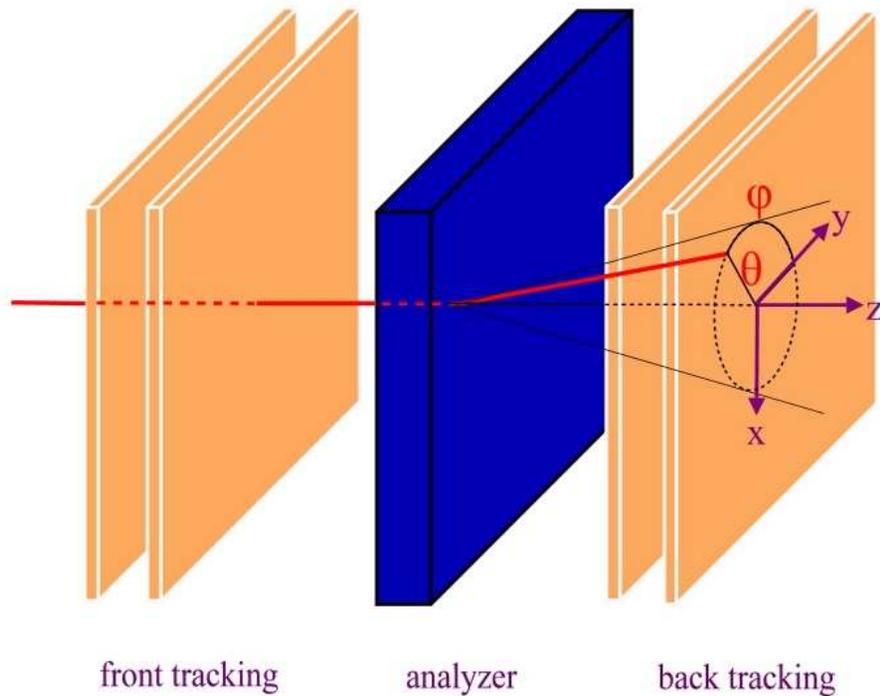
# E04-108 – FPP

Newly constructed  
**Focal Plane**  
**Polarimeter** installed  
into HMS



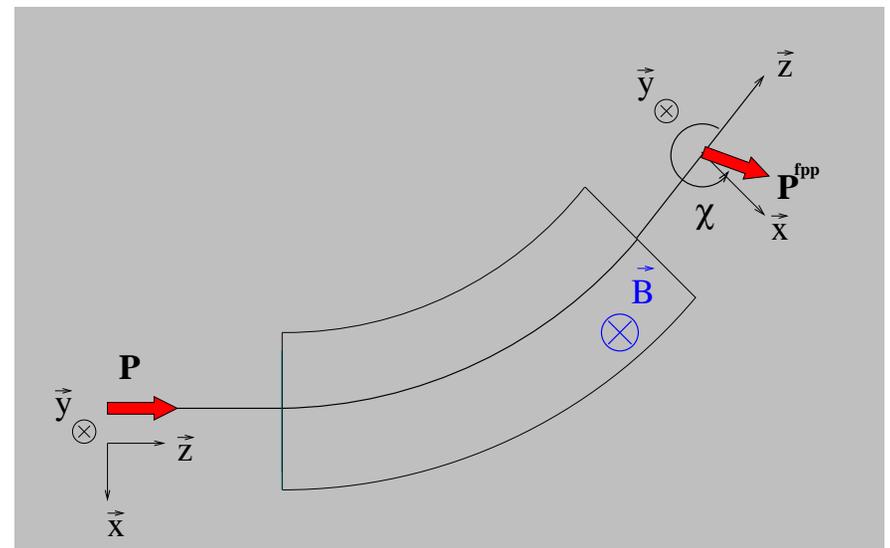
2 polarimeters in succession enhance efficiency

# E04-108 – Polarimetry

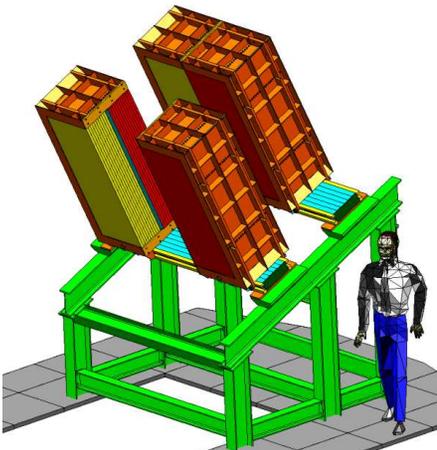


Polarimeter measures polarization dependent re-scattering

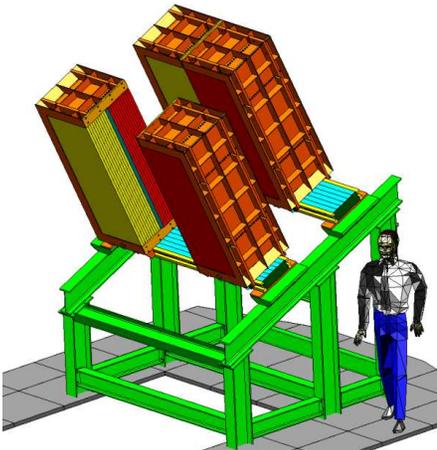
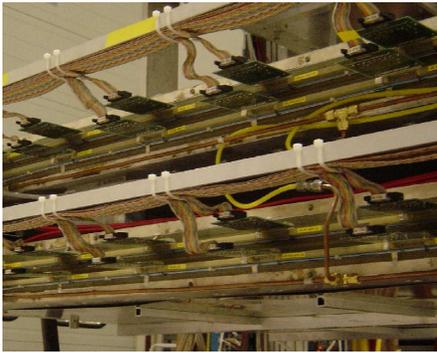
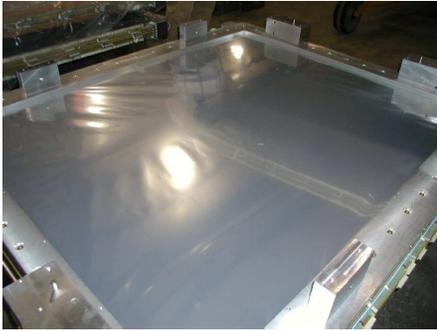
Polarization vector precesses in magnetic dipole and quadrupole fields



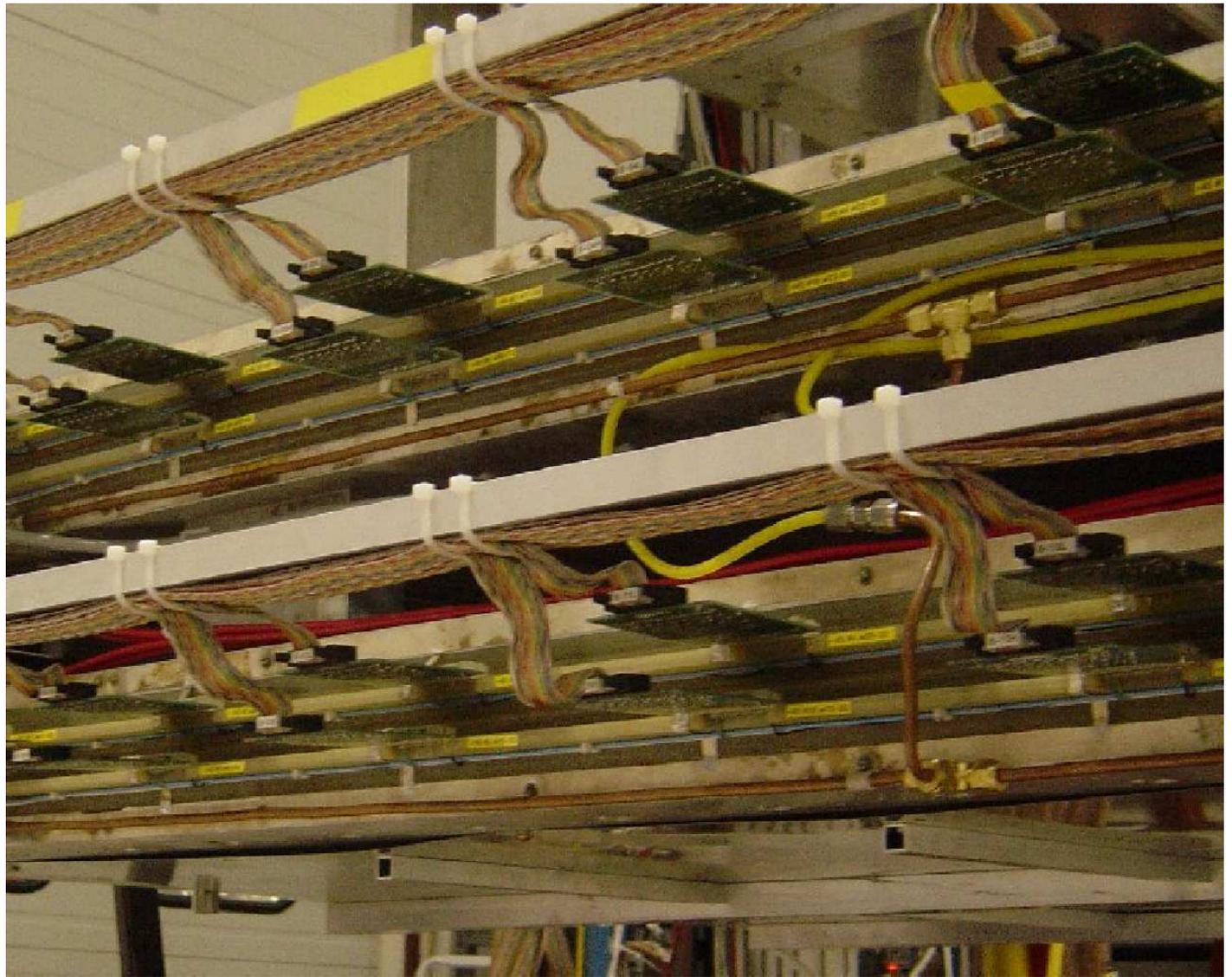
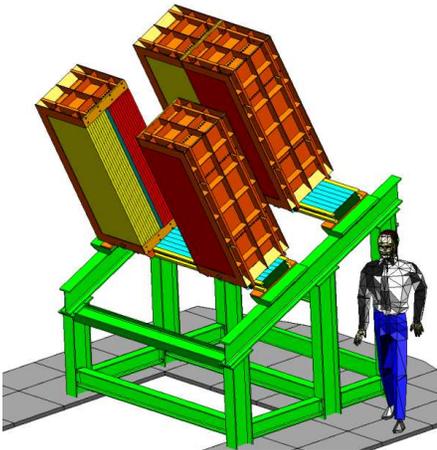
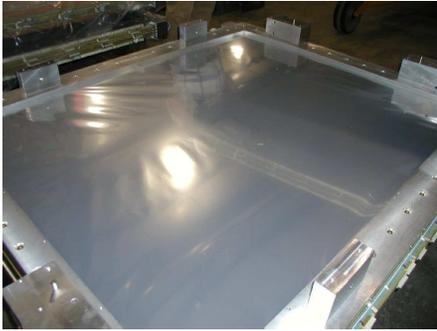
# E04-108 – FPP



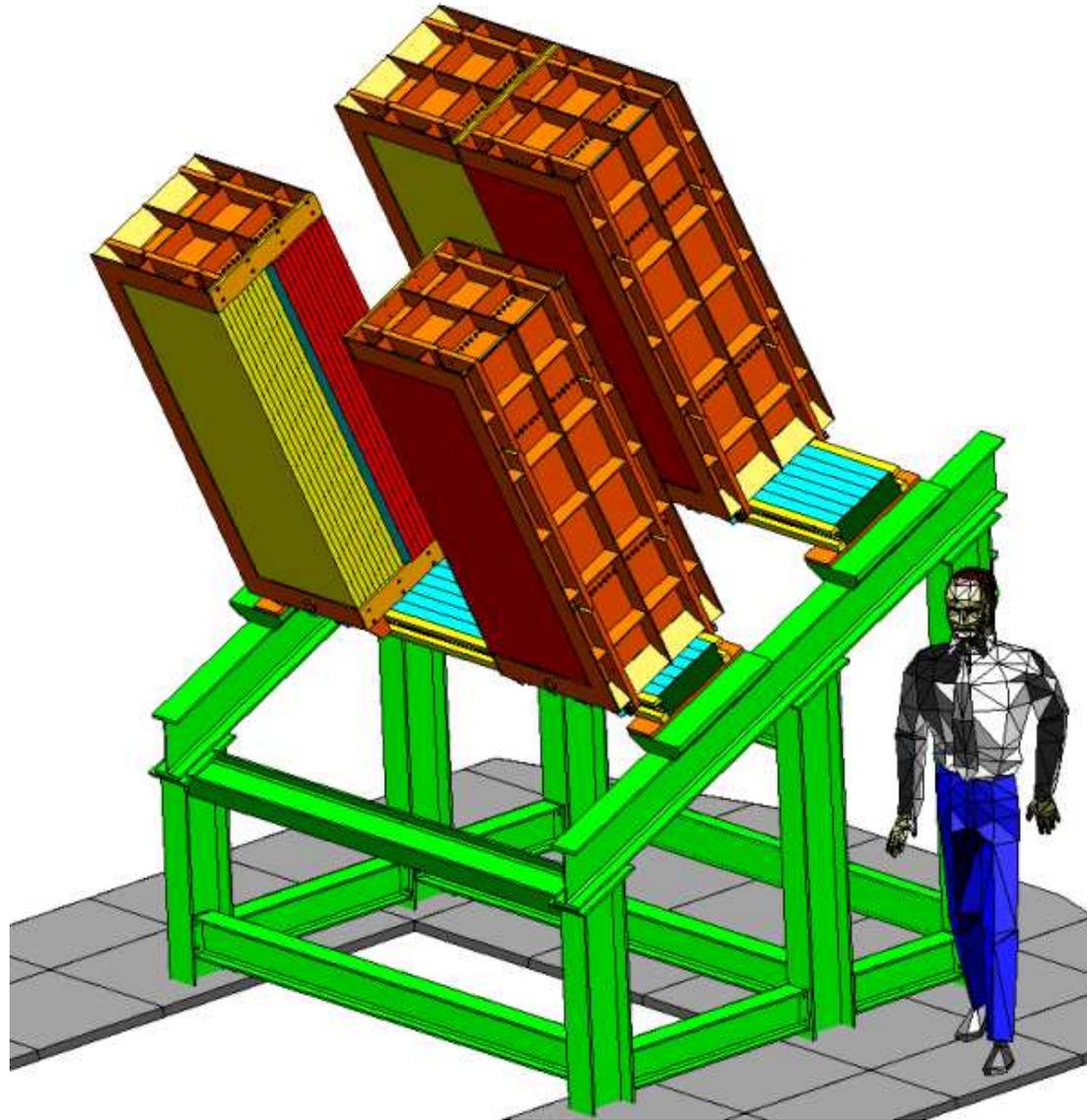
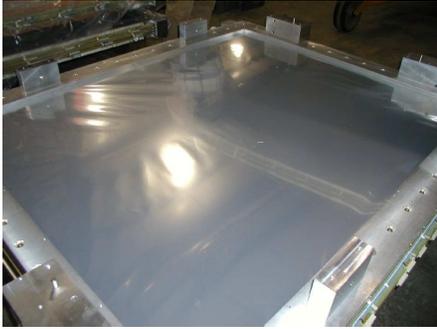
# E04-108 – FPP



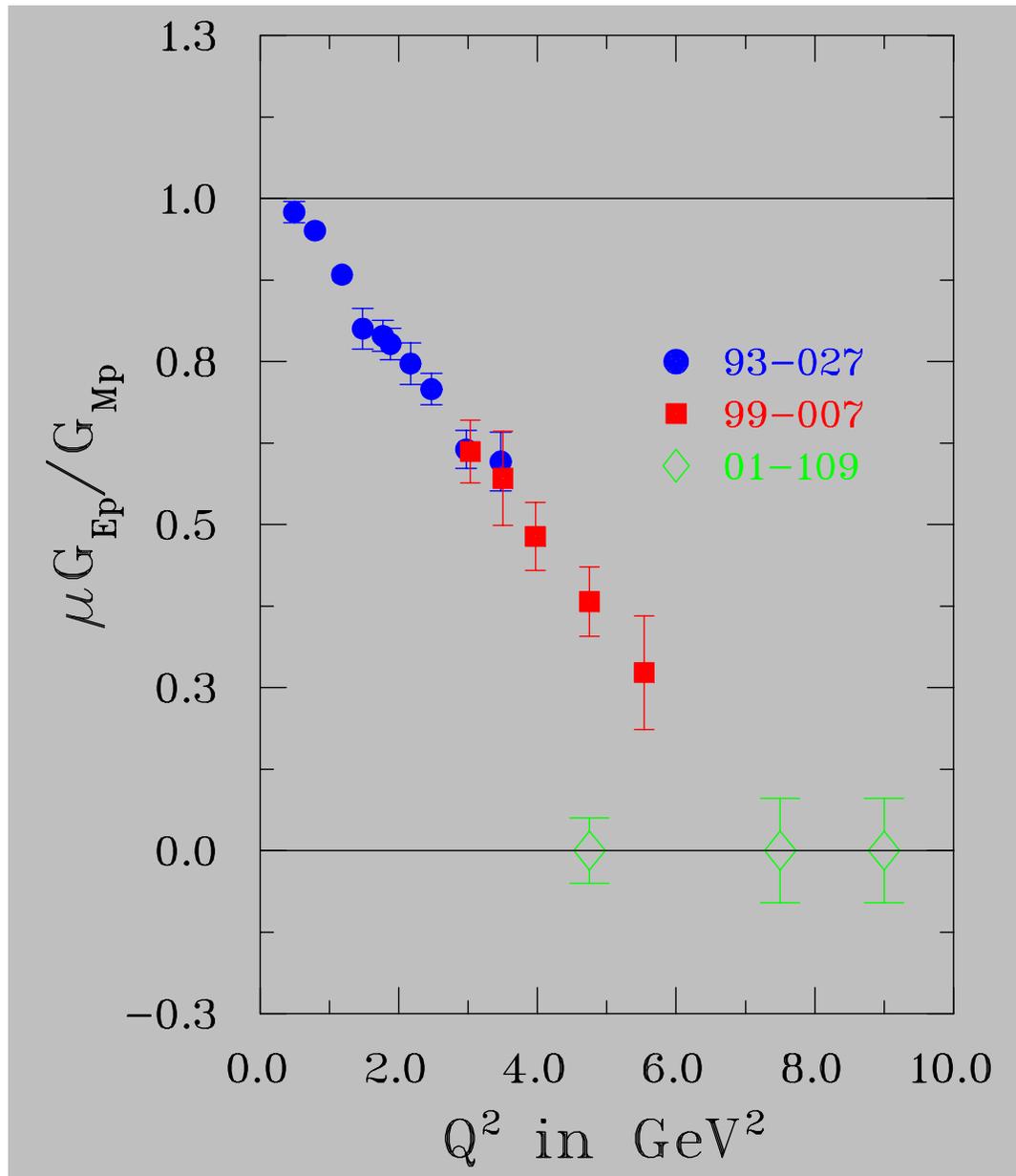
# E04-108 – FPP



# E04-108 – FPP



# *E04-108 – Expected Results*



- Expands upon spectacular Hall A results
- Sister experiment: dedicated  $2\gamma$  measurement
- scheduled for 2007/2008

# Summary

- Form Factors are Vital to Our Understanding of Nature
- Many Experiments have Already been Undertaken
  - *limited kinematic range*
- Comprehensive theory model lacking
  - *higher  $Q^2$  data?*
- Significant Contribution from Jefferson Lab
  - *recent  $G_E^n$  measurement in Hall A*
  - *upcoming  $G_E^p/G_M^p$  in Hall C*
  - *extensive weak FF program ( $G^0, Q_{\text{weak}}$ )*